

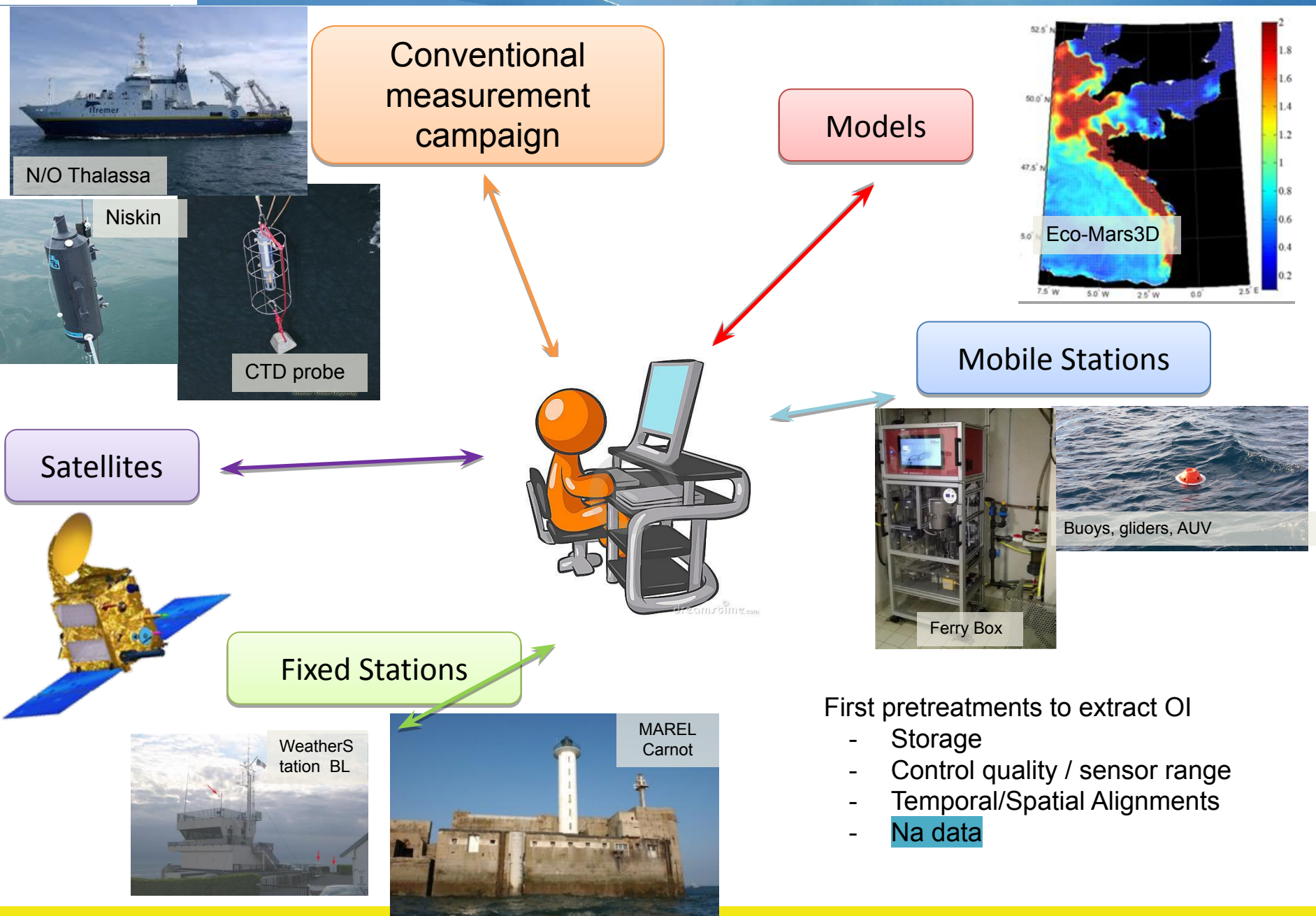
Missing data
DTW-based imputation

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First pretreatments to extract OI

- Storage
- Control quality / sensor range
- Temporal/Spatial Alignments
- **Na data**

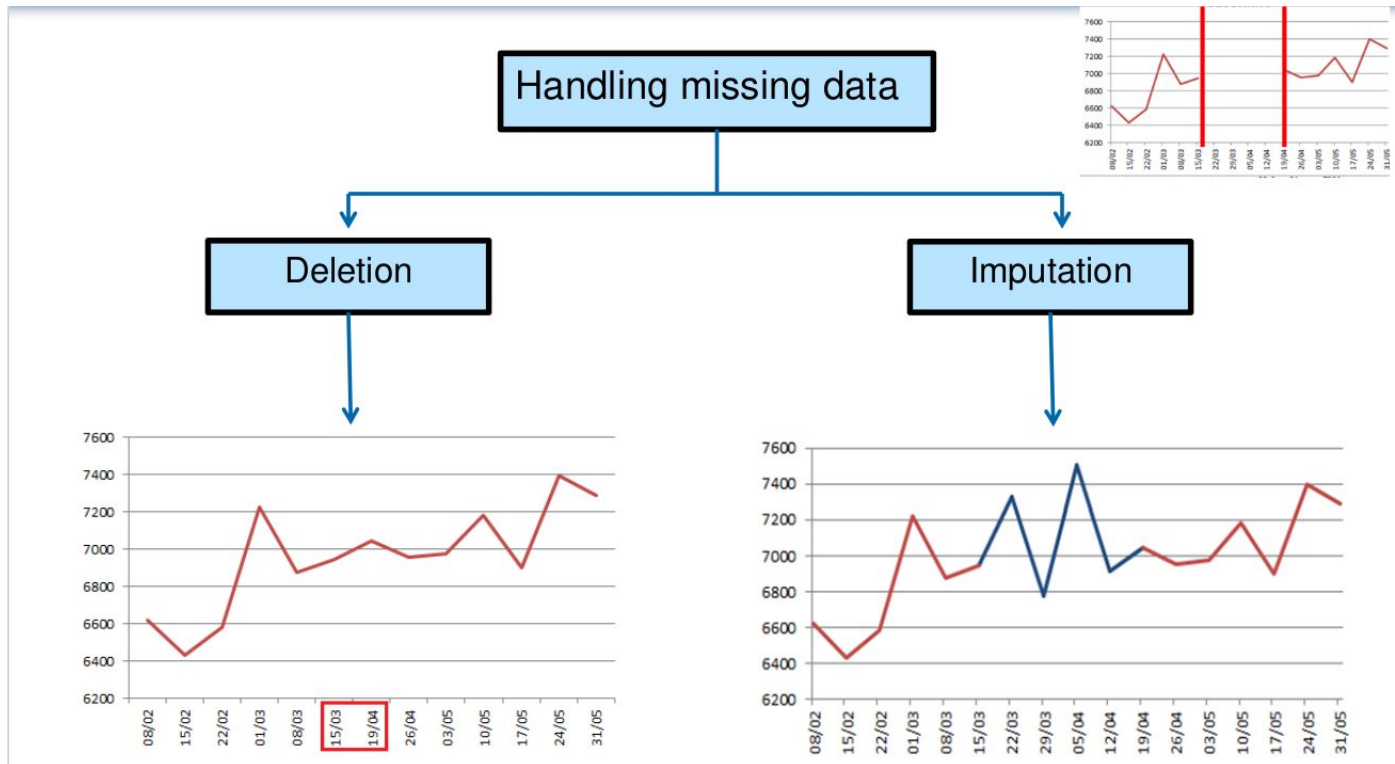
Collecting lots of time series data (big data)

Problems:

- Collected data have missing values due to sensor or communication/transmission problems
- Most of Classification and prediction tools require completed data

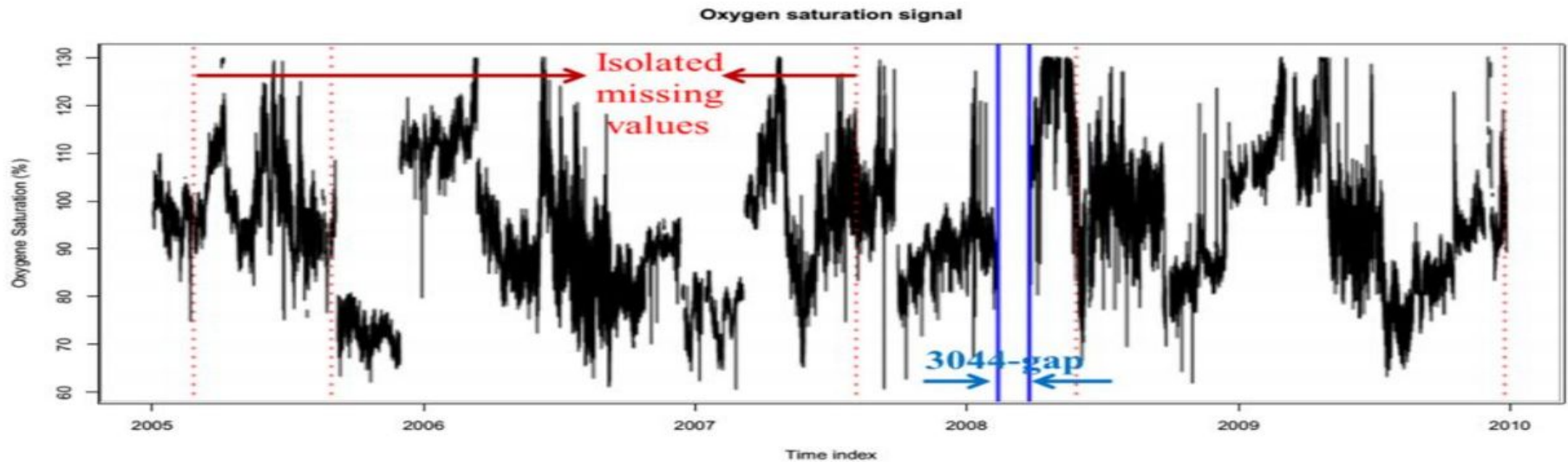
Any available solution?

- Deleting some observations
- Imputation data



Which methods to deal with missing marine observations ?

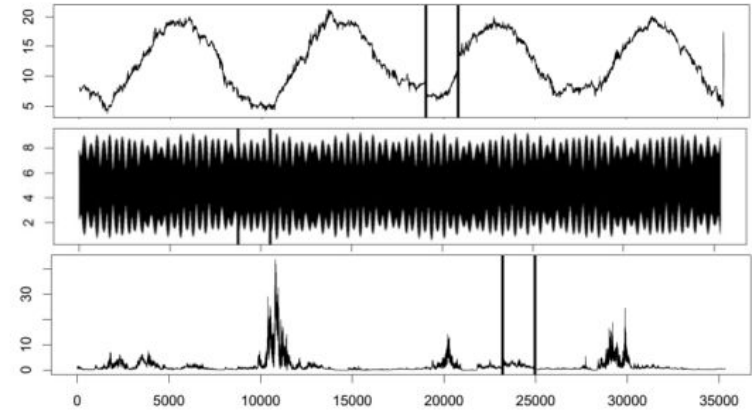
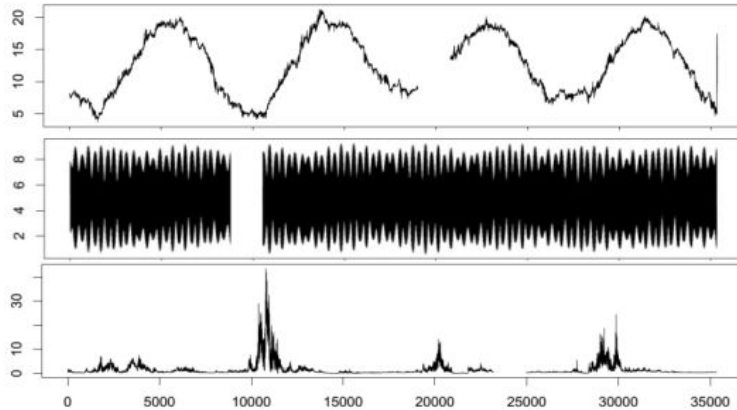
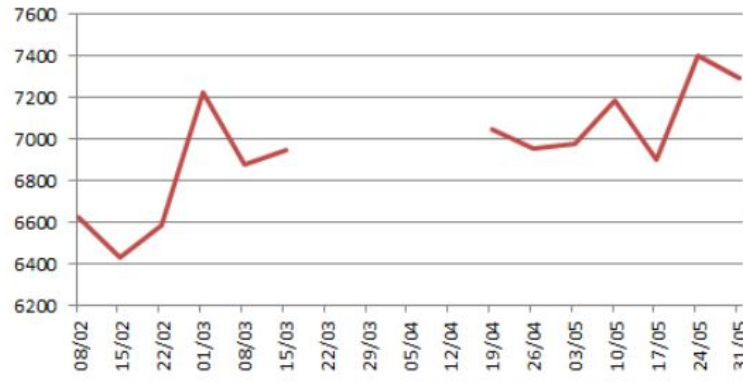
- 1- Nature of the missing data : MCAR, MAR, NMAR ↔ not so easy to define.
- 2- Isolated missing values / Gap=missing consecutive values
- 3- Complex data, low cross-correlation
- 3- Quick change in the dynamics of the studied process.



=> Adapted algorithm, **results must be**

- **efficient**: having minimal standard errors
- **reliable/effective**: respecting curve-shape and dynamics process/changes.

Which methods to deal with missing marine observations



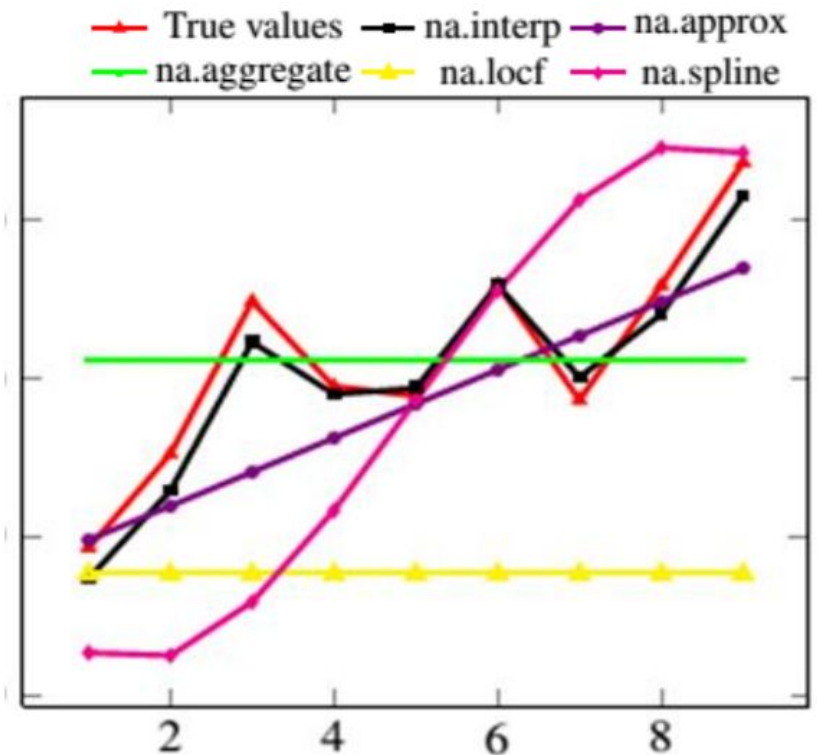
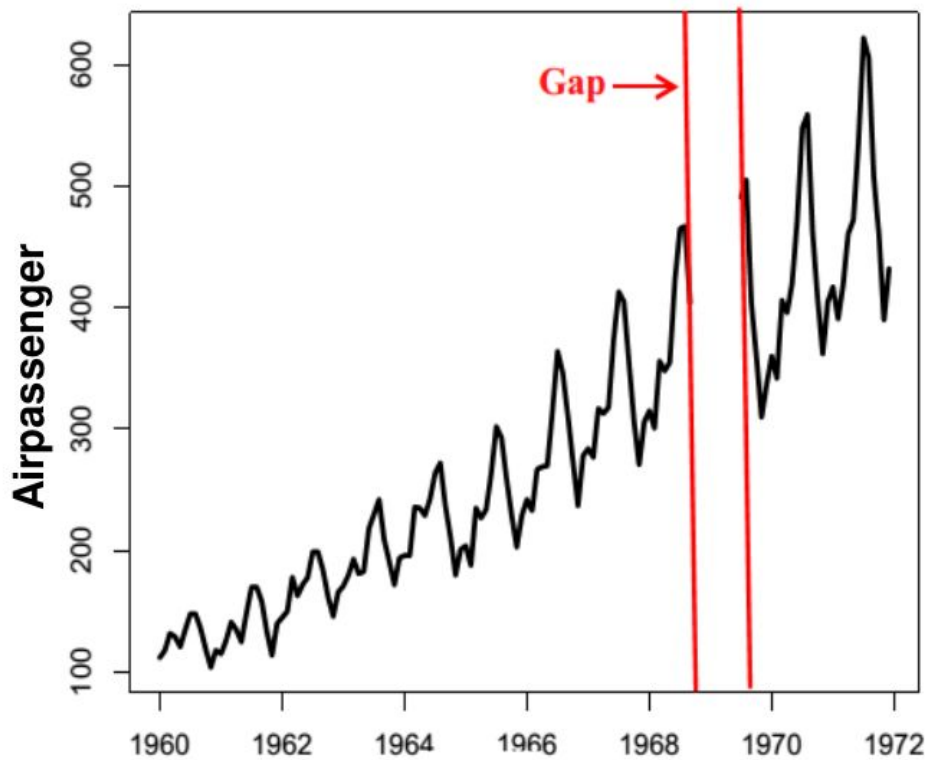
=> Adapted algorithm, **results must be**

- **efficient**: having minimal standard errors
- **reliable/effective**: respecting curve-shape and dynamics process/changes.

Case of Isolated missing values in **univariate times series**

-> Usual methods : local averages, interpolation, regression.

But for gap ?



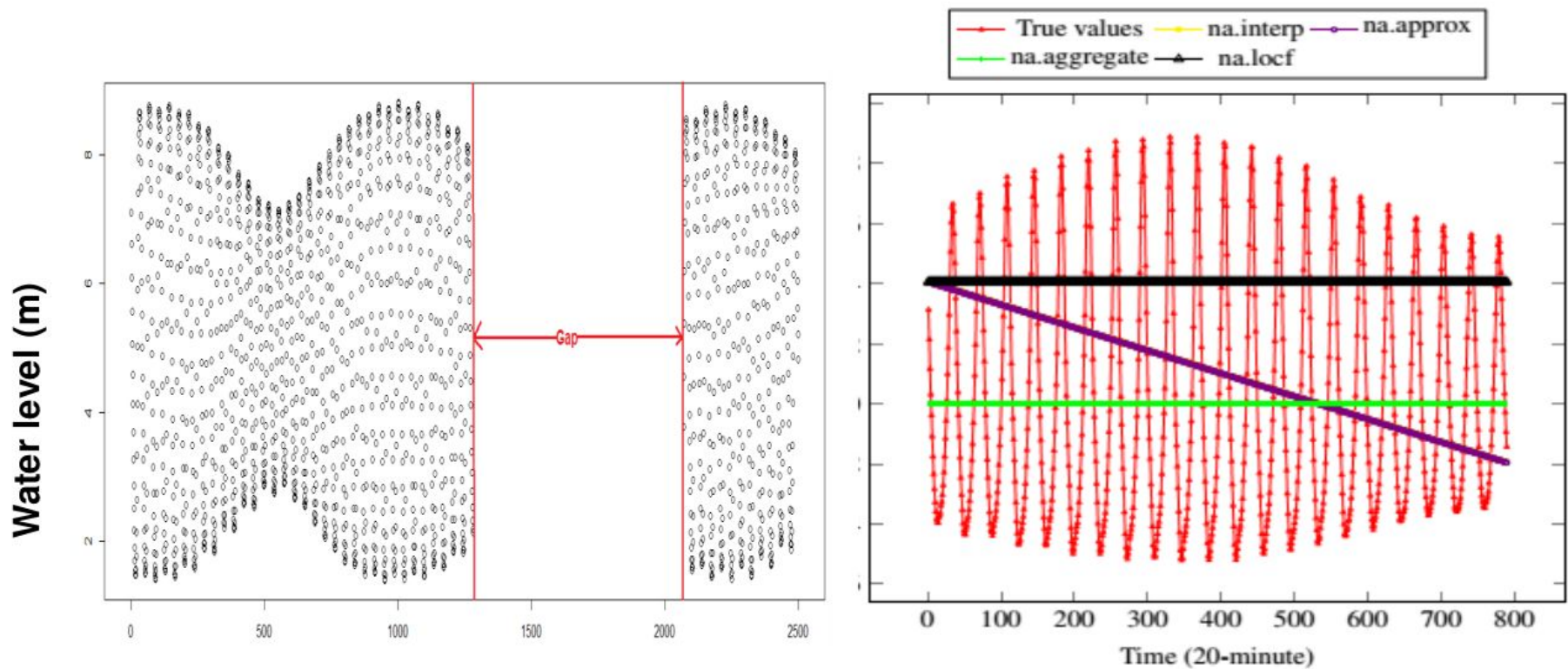
Kaggle dataset. **Univariate** time series.

na.interp only respects the **pattern shape**

Solution for Isolated missing values in **univariate times series**

-> Usual methods : local averages, interpolation, regression.

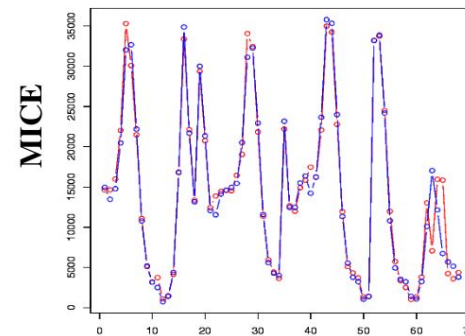
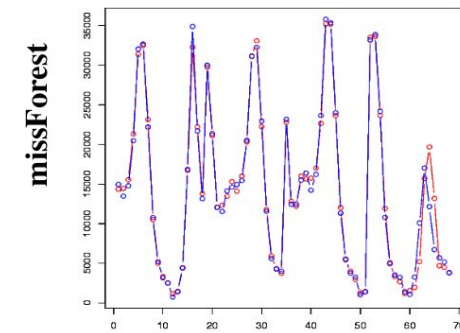
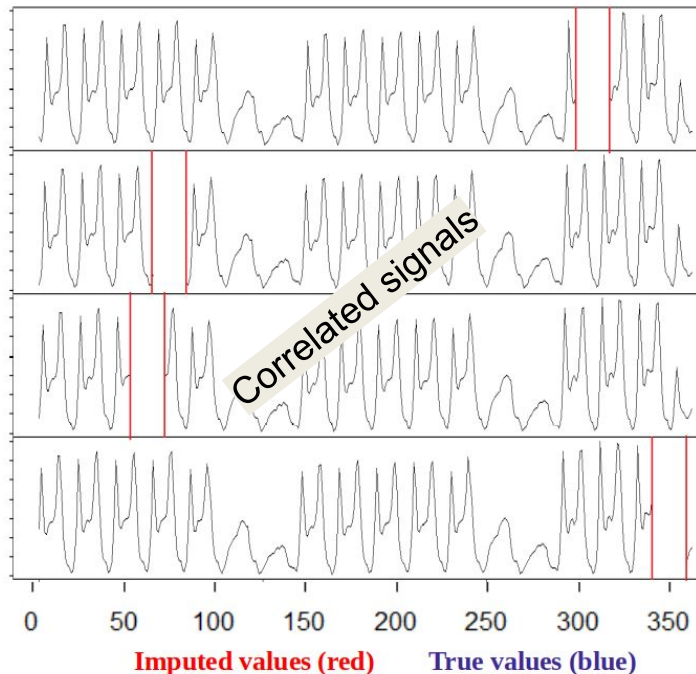
And large gap ?

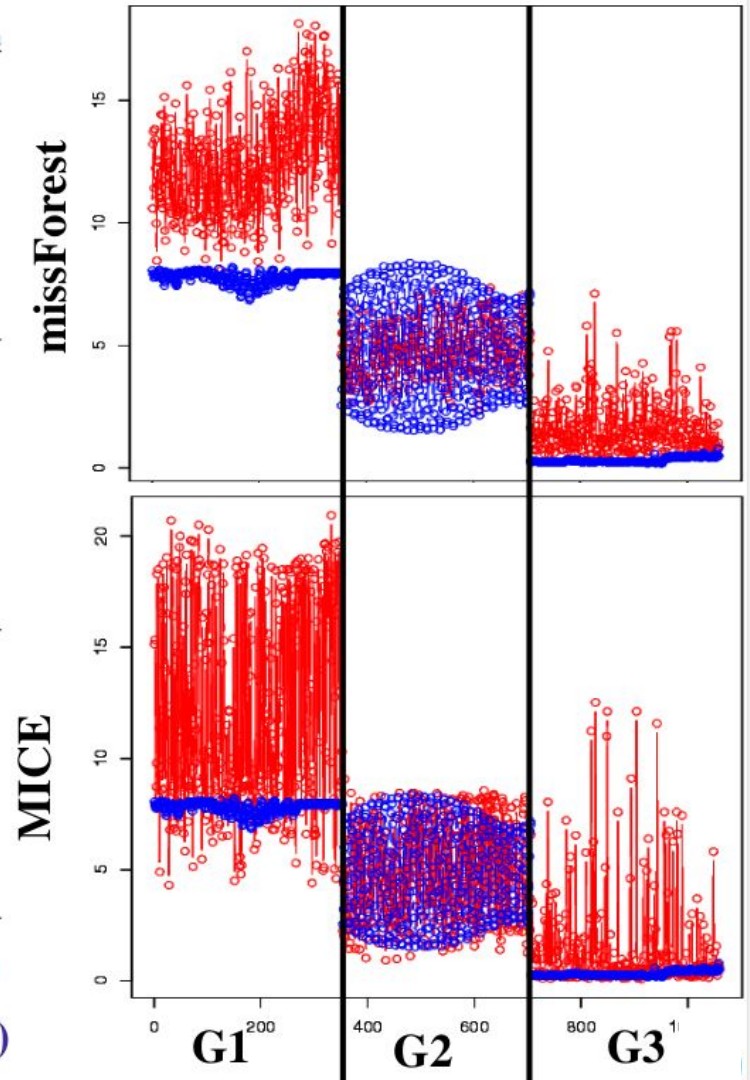
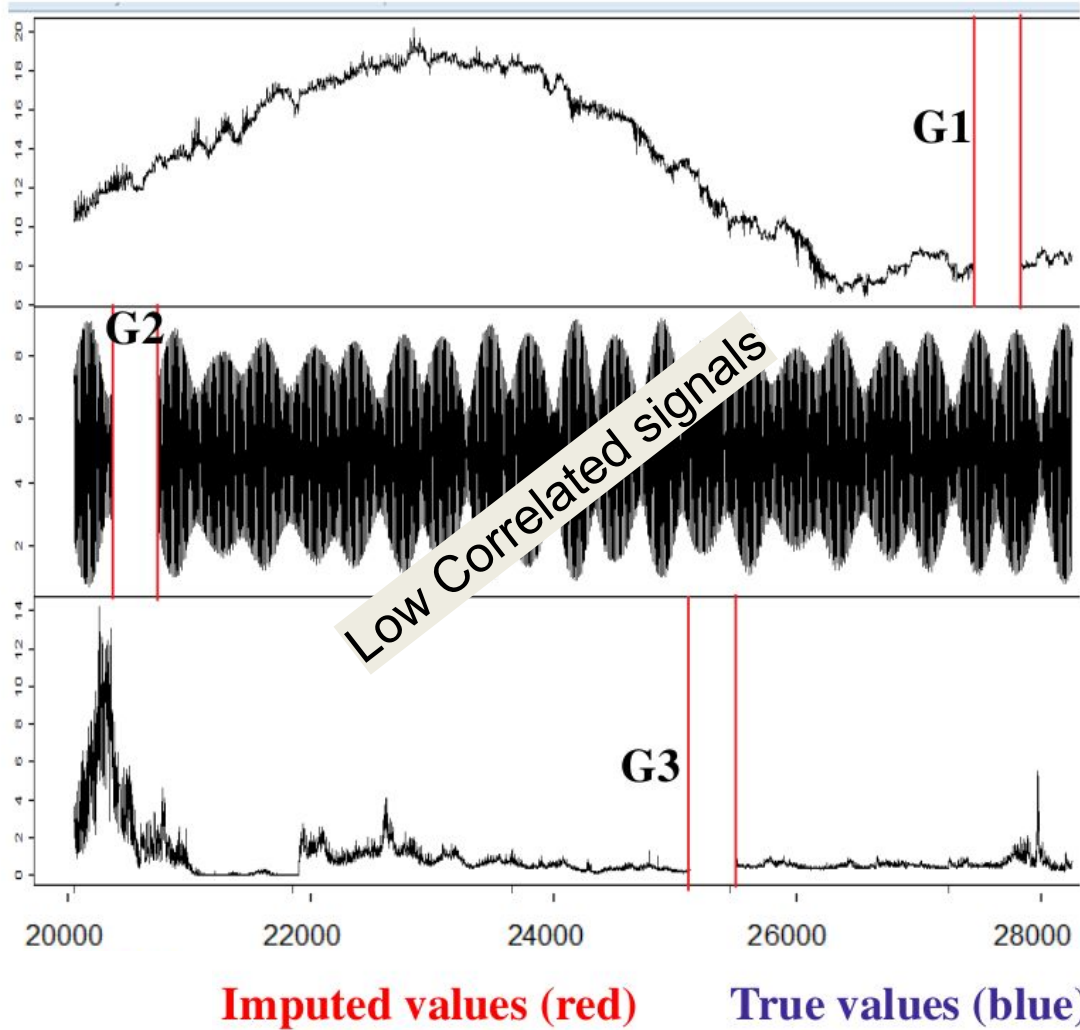


Efficient but no respect for the pattern shape.

Solution for multivariate times series

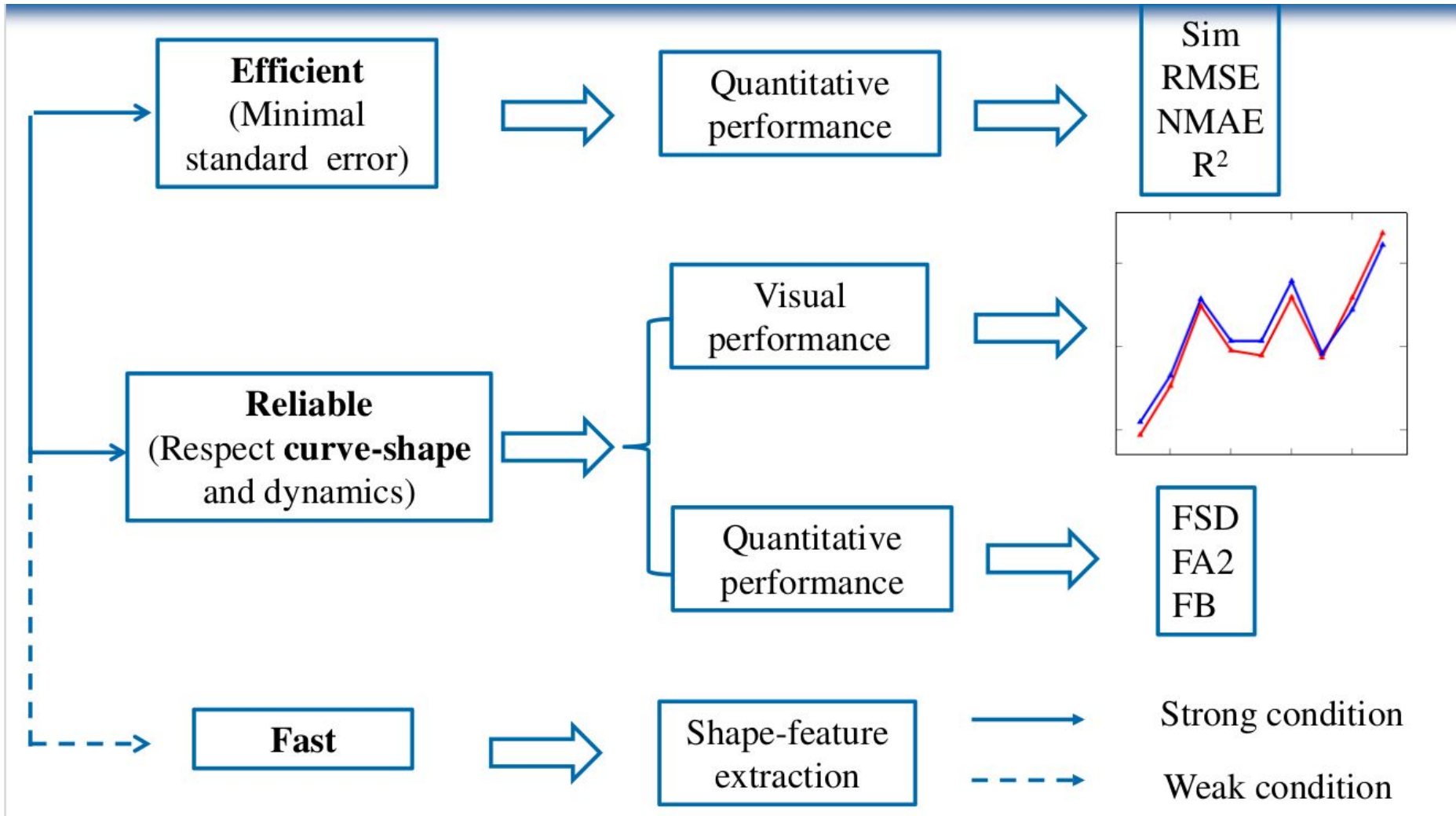
- **MI - Multiple Imputation**: predicts imputed value by finding an observation (from available values) with the closest predictive mean to that variable containing missing values for each observation.
- **MICE - Multivariate Imputation via Chained Equations**: estimate imputed values based on the conditional distribution (on all of other variables) for each variable containing missing values.
- **na.approx** (zoo package): uses a generic function with interpolated values to estimate each missing data.
- **missForest**: for each variable missForest builds a random forest model on the observed part. Then this model is used to predict missing values in the variable. (look at the code : fill by means !)
- **k-nearest neighbors**





-> No efficiency / no shape respect for large gap

Goal and Trade off.



Idea

Proposed approach

Focus on Marel Carnot Dataset

Dataset
MAREL Carnot

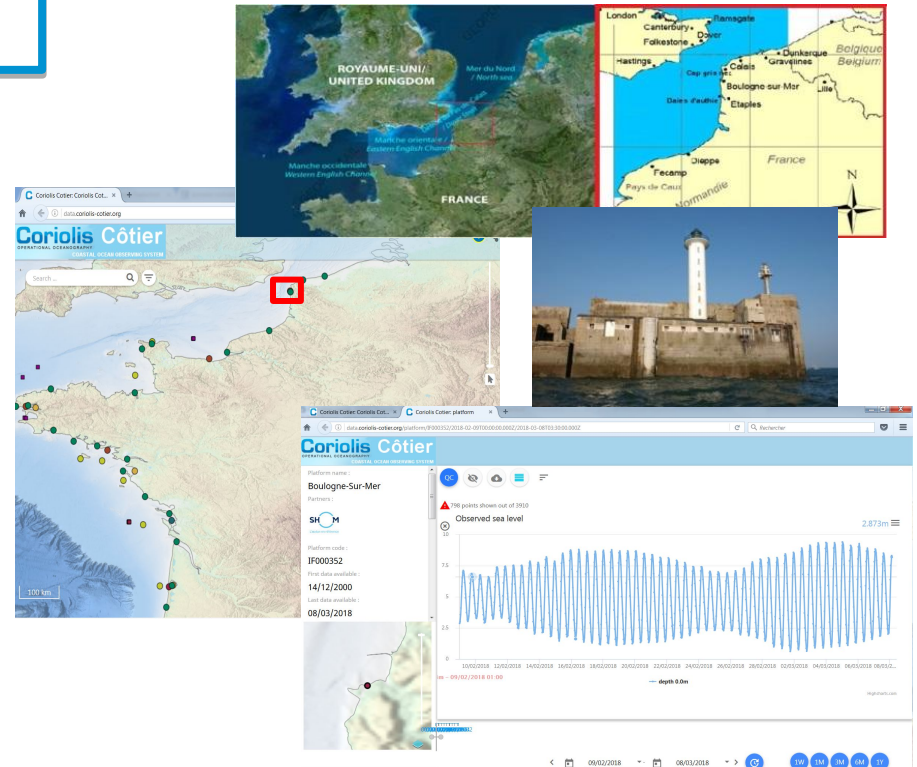
High frequency instrumented station (HF)
20 minutes sampling

Tests based on 4 years (2005-2009)

Raw Data
Size : 92 968 * 9
#NA: 320 401 : 38 %

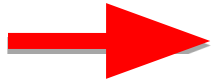
9 Essential Ocean Variables :

- Temperature
- Salinity
- Dissolved Oxygen
- Nitrate
- Phosphate
- Silicate
- Turbidity
- PAR (Photosynthetically Active Radiation)
- Fluorescence



<http://data.coriolis-cotier.org/>

Completion Protocol:



T-gap: size T of consecutive missing values



completion size criterion: smallHole and acceptedHole

Completion steps:

- 1- Isolated points (T=1)-gap: completion by local average (t-1 and/or t+1)
- 2- small T-gap: completion by weighting local average of a mobile centered windows [t-T; t +T]
T < smallHole
- 3- large T-gap: filling by existing recurrent pattern with DTW-matching
(smallHole < T ≤ acceptedHole)

smallHole , acceptedHole depends on

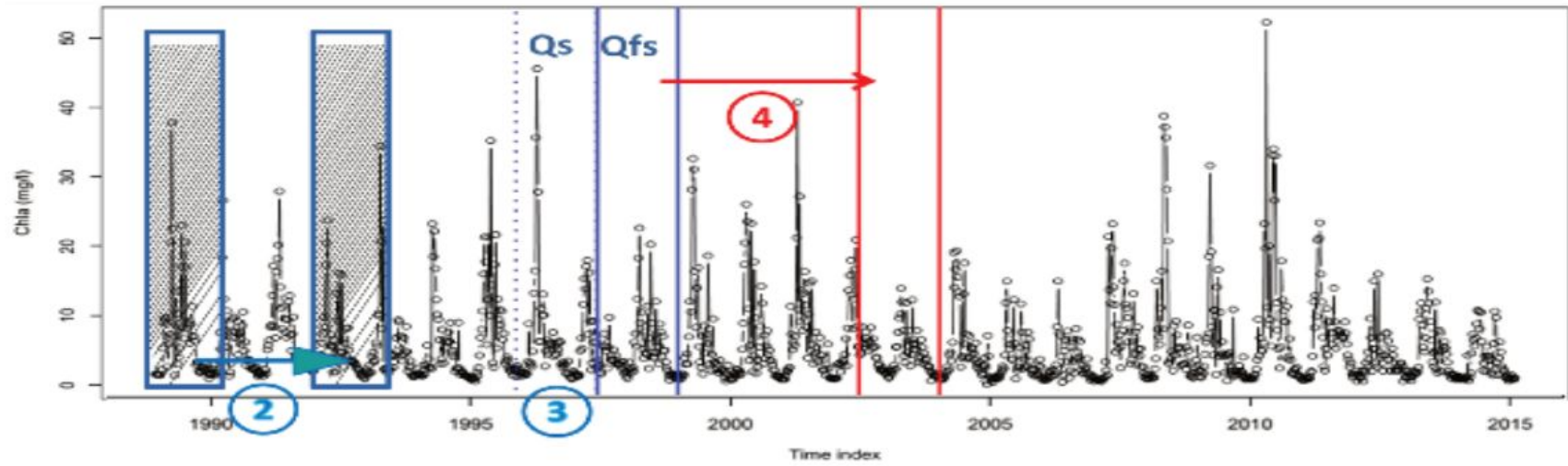
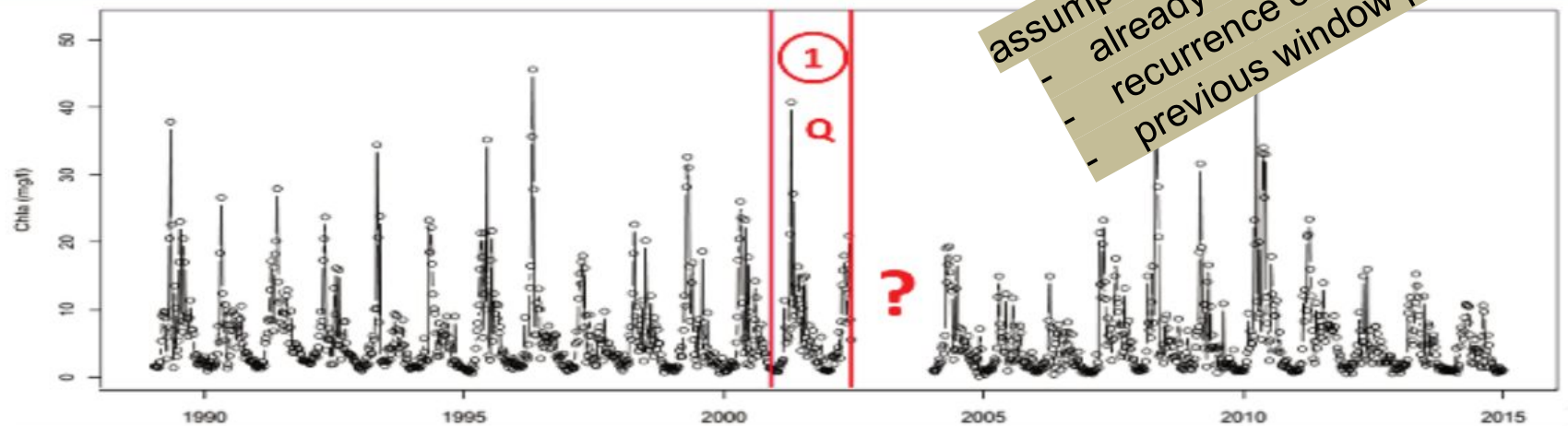
- dynamics change
- subject of interest.

Proposed approaches for large $T \gg 1$ -gap:

- DTWBI : univariate iseries - imputation based on DTW criterion
- DTWUMI : extension of DTWBI for multivariate series
- FSMUMI : Fuzzy Logic Theory
- eDTWBI : add trend conservation constraints + future window

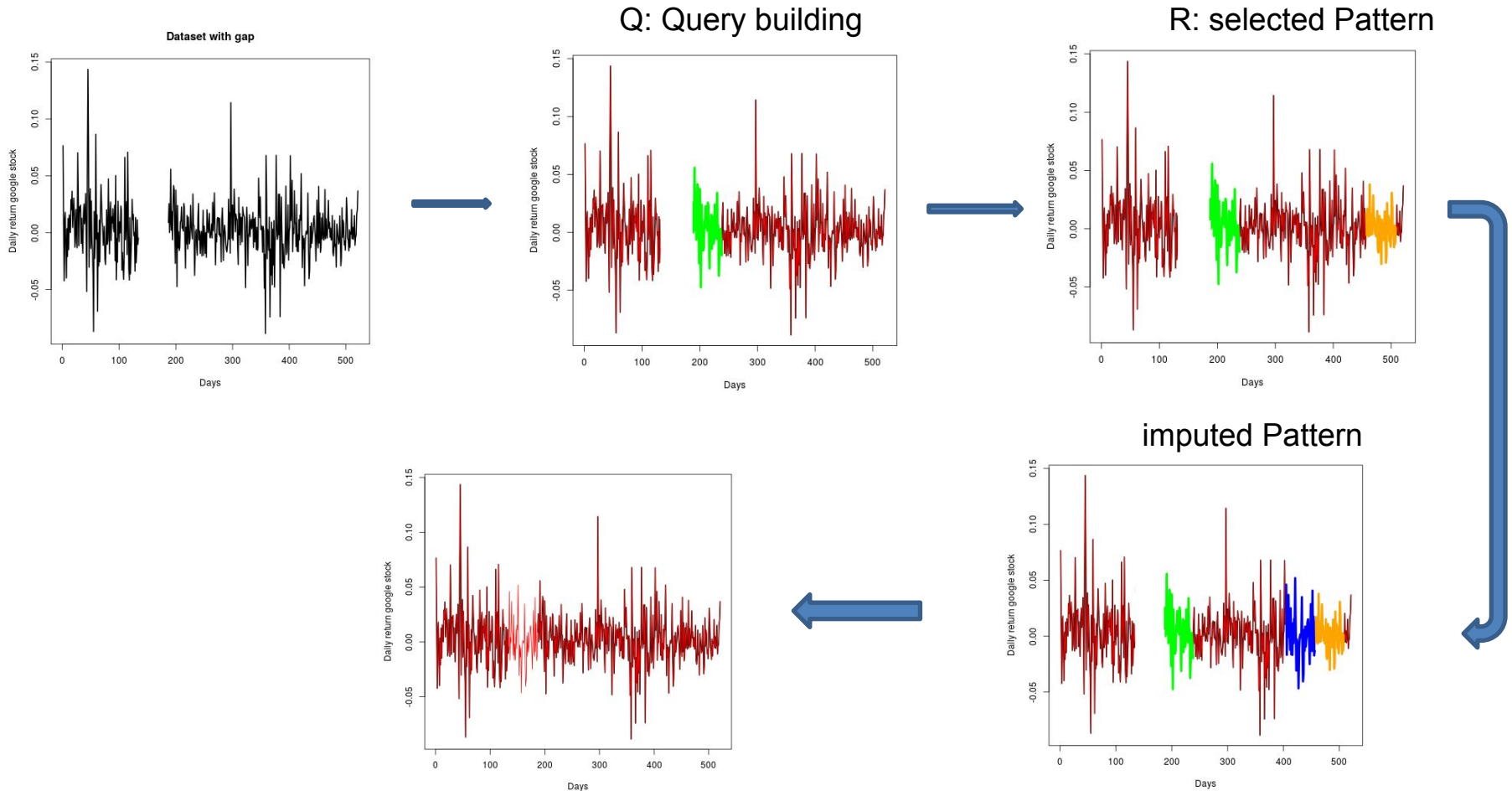
assumption :

- already existing information
- recurrence of phenomena
- previous window pressure

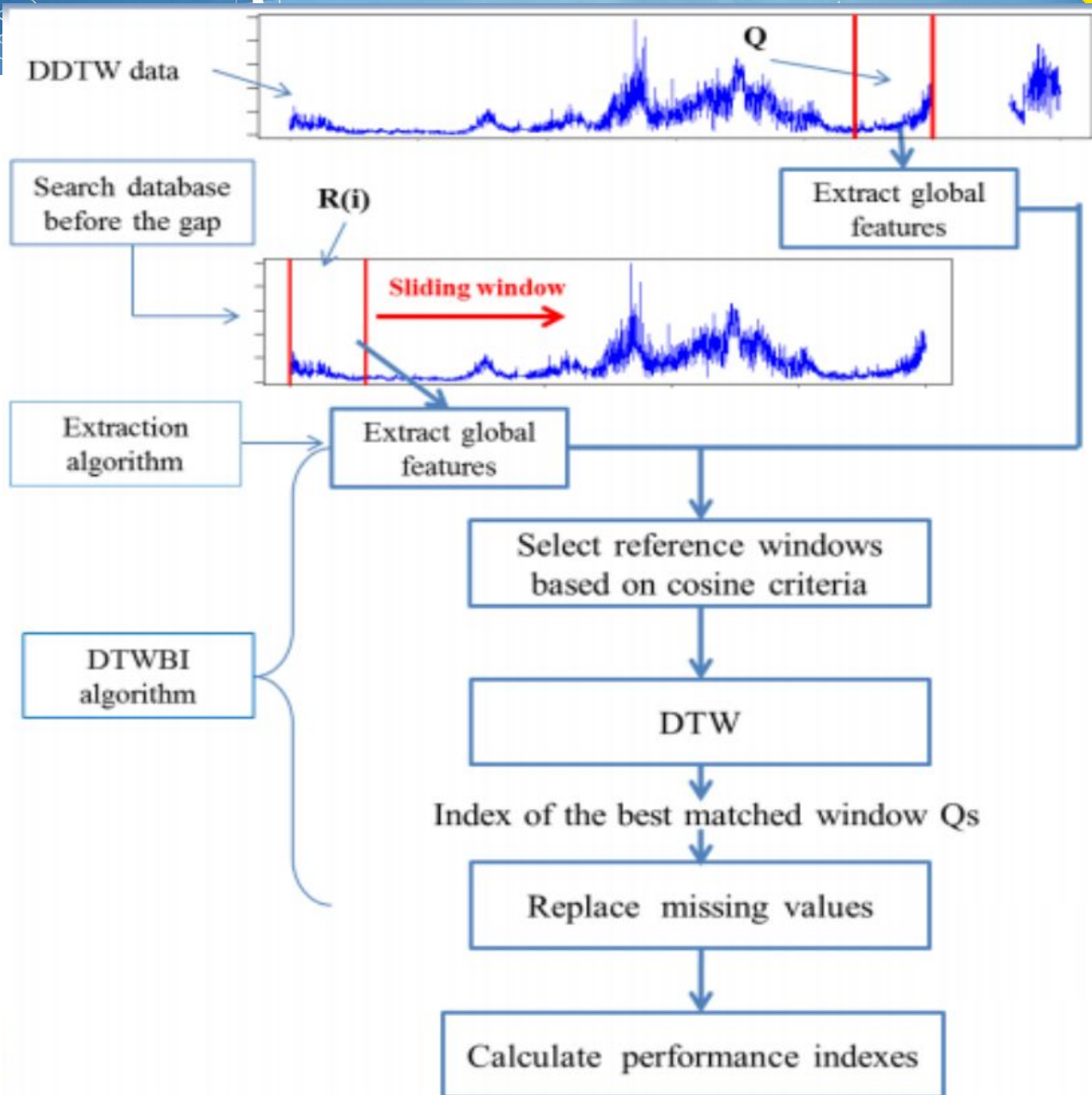


Illustration/Vocabulary:

Completion of one large gap by “DTW-similar” recurring pattern



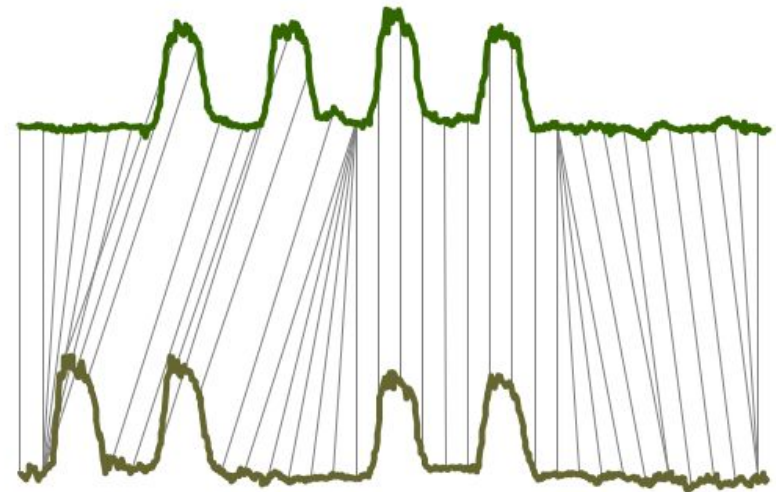
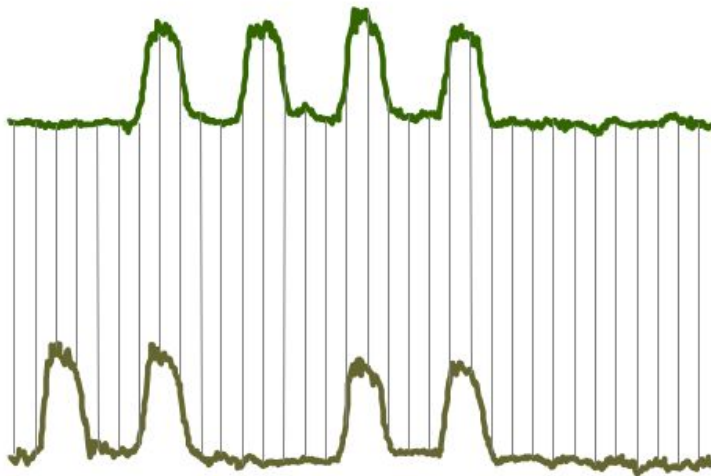
Univariate signal



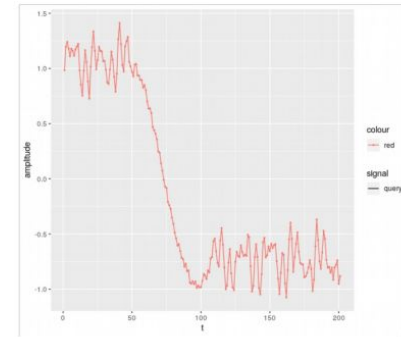
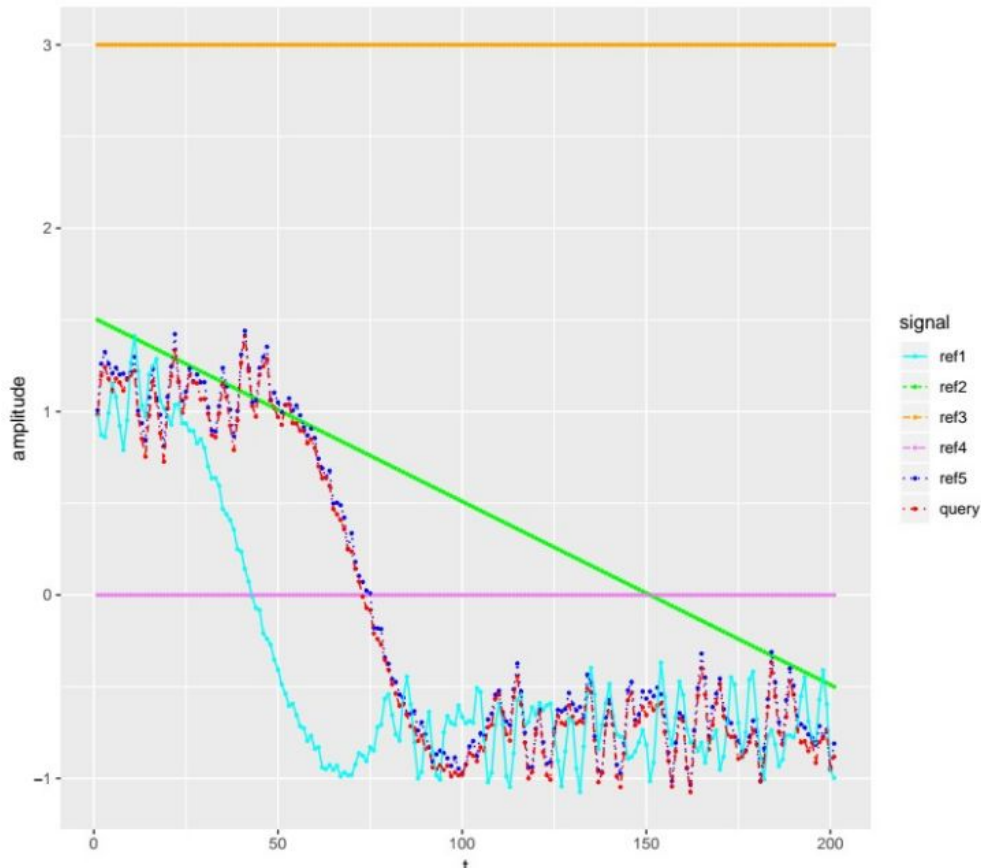
Similarity problem

- Given: two sequences $X = \{x_1, x_2, \dots, x_n\}$ and $Y = \{y_1, y_2, \dots, y_m\}$
- How to define and compute $\text{Sim}(X, Y)$ according to acceptable time variability?

Euclidean distance vs. DTW



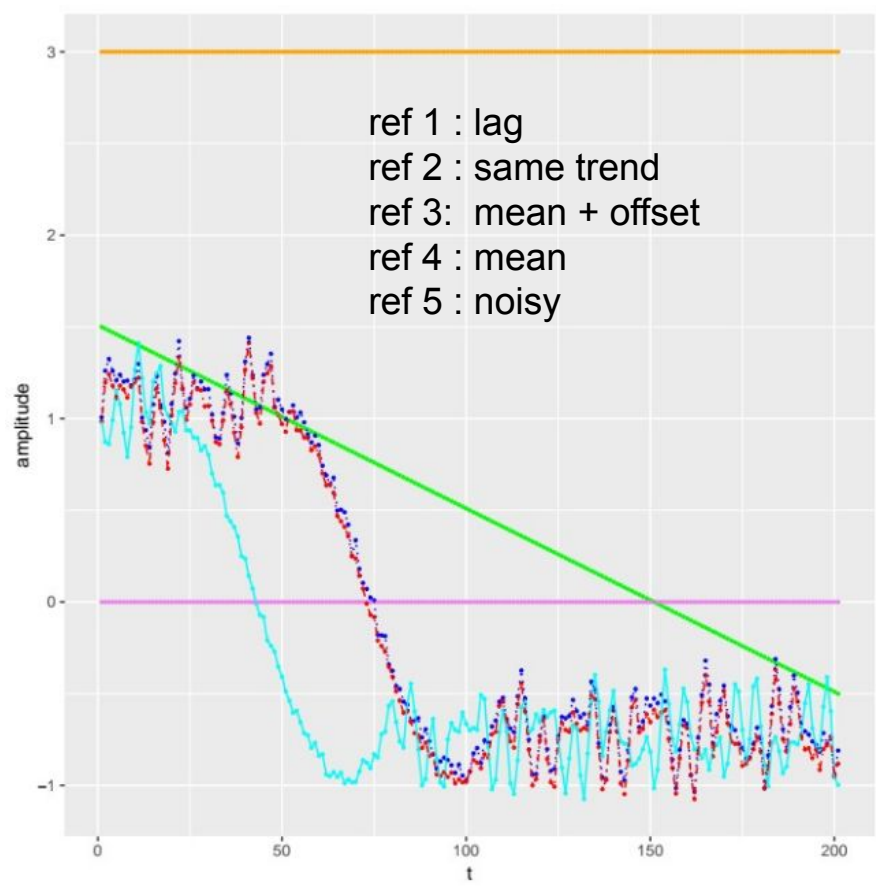
Signal comparison - **Euclidean distance** Metrics ?



ref 1 : lag
 ref 2 : same trend
 ref 3: mean + offset
 ref 4 : mean
 ref 5 : noisy

	query	ref1	ref2	ref3	ref4	ref5
distMax	0.00	1.64	1.53	4.07	1.41	0.10
ME	0.00	0.27	-0.63	-3.13	-0.13	-0.05

Signal comparison - Euclidean distance Metrics ?



ref 1 : lag
ref 2 : same trend
ref 3: mean + offset
ref 4 : mean
ref 5 : noisy

GMV=VG	$\exp(\overline{(\ln(q) - \ln(r))^2})$	min.	$\in \mathbb{R}^+$	$+ 0.75 \leq VG \leq 1.25$
FA2	$\frac{1}{T} \text{card}(0.5 \leq q_i / r_i \leq 2)$	max.	$\in [0, 1]$	$+ FA2 > 0.8$
R ² Pearson	$(\frac{\text{cov}(q,r)}{\sigma_q \times \sigma_r})^2$	max.	$\in [0, 1]$	$++ R^2 \geq 0.9$ p-value
FB	$2 \times \frac{\bar{q} - \bar{r}}{\bar{q} + \bar{r}}$	min.	$\in [-2, 2]$	$++ FB \leq 0.3$
GMB=BG	$\exp(\overline{\ln(q) - \ln(r)})$	min.	$\in \mathbb{R}^+$	$+ 0.75 \leq BG \leq 1.25$
FS	$2 \times \frac{ (\sigma_q)^2 - (\sigma_r)^2 }{(\sigma_q)^2 + (\sigma_r)^2}$	min.	$\in [0, 2]$	$++ FS \leq 0.5$
FSD	$2 \times \frac{\sigma_q - \sigma_r}{\sigma_q + \sigma_r} $	min.	$\in [0, 2]$	$++ FSD \leq 0.5$

signal
 - ref1
 - ref2
 - ref3
 - ref4
 - ref5
 - query

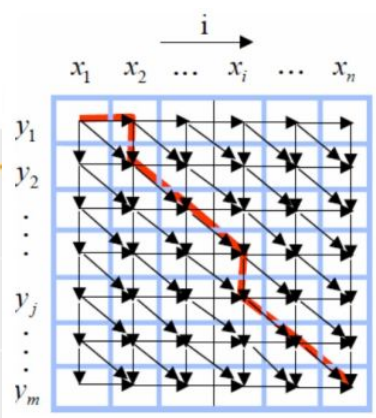
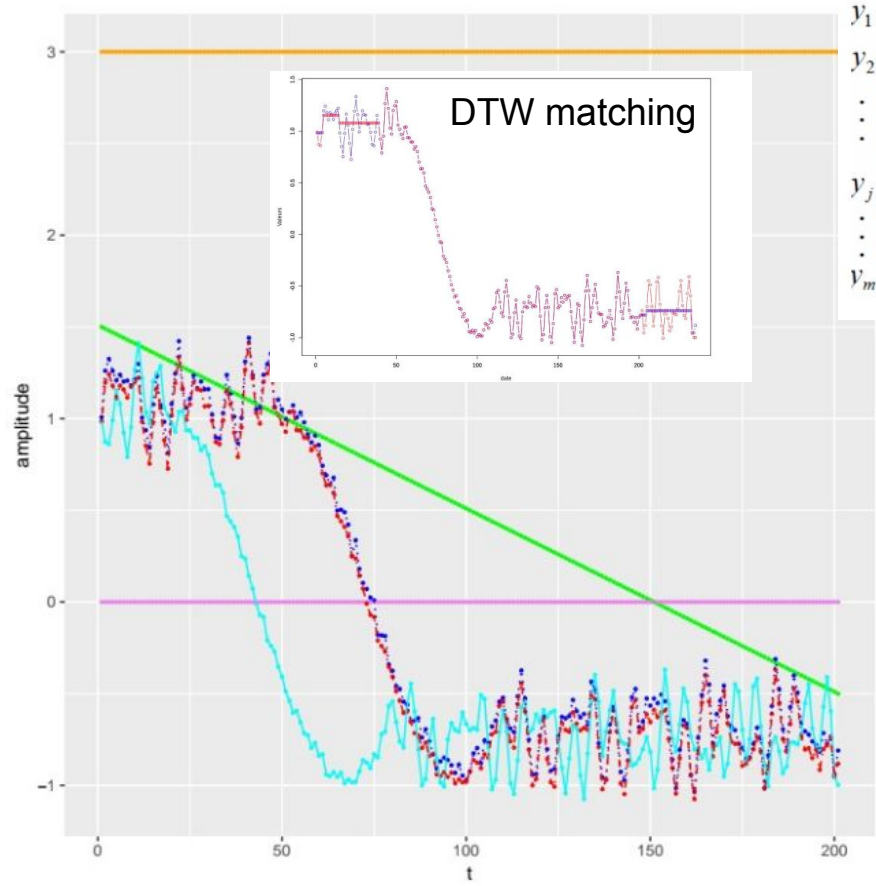
bounded scores

Bold results = criterion is satisfied

	query	ref1	ref2	ref3	ref4	ref5
distMax	0.00	1.64	1.53	4.07	1.41	0.10
ME	0.00	0.27	-0.63	-3.13	-0.13	-0.05
VG	1.00	14.71	12.71	137.54	-	1.02
FA2	1.00	0.78	0.41	0.00	0.00	0.99
R2.cor	1.00	0.55	0.72	0.00	0.00	1.00
Bias	0.00	0.27	-0.63	-3.13	-0.13	-0.05
FB	0.00	-1.04	-3.33	-2.17	2.00	0.55
BG	1.00	1.33	0.78	0.18	-	0.98
FS	0.00	0.41	0.69	2.00	2.00	-0.00
FSD	0.00	0.21	0.36	2.00	2.00	0.00

-> no signal satisfies all criteria

Signal comparison - Elastic matching Metrics ?



$$X = \{(x_i), i = 1, \dots, n\}$$

$$Y = \{(y_j), j = 1, \dots, m\}$$

$$P = \{(i_k, j_k), k = 1, \dots, n_k\}$$

$$C(X, Y, P, W) = \frac{\sum_{k=1}^{n_k} d(x_{i_k}, y_{j_k}) \cdot w(k)}{\sum_{k=1}^{n_k} w(k)}$$

$$= \frac{Dist(n, m)}{\sum_{k=1}^{n_k} w(k)}$$

Elastic matching
Deformation tolerance
DTW / Derivative DTW / Features DTW

	VG	FA2	R2.cor	FB	BG	FS	FSD
ref1-DTW	1.04	1.00	0.99	0.04	1.01	-0.01	0.00
ref1-DDTW	1.08	1.00	0.98	-0.05	0.97	0.14	0.07
ref1-AFBTDTW	1.06	1.00	0.99	-0.03	1.02	0.05	0.03
ref2-DTW	g.	0.96	0.96	-0.47	89.37	0.23	0.11
ref2-DDTW	83.98	0.41	0.33	-8.43	1.57	-0.50	0.25
ref2-AFBTDTW	3.63	0.42	0.92	-2.84	1.35	0.05	0.03
ref3-DTW	12.08	0.00	0.00	-1.30	0.39	2.00	2.00
ref3-DDTW	g.	0.00	0.00	-2.87	0.09	2.00	2.00
ref3-AFBTDTW	g.	0.00	0.00	-2.70	0.14	2.00	2.00
ref4-DTW	g.	0.00	0.00	2.00	g.	2.00	2.00
ref4-DDTW	g.	0.00	0.00	2.00	g.	2.00	2.00
ref4-AFBTDTW	g.	0.00	0.00	2.00	g.	2.00	2.00
ref5-DTW	1.04	0.99	1.00	0.19	1.07	-0.00	0.00
ref5-DDTW	1.05	0.94	0.99	0.68	0.99	-0.05	0.03
ref5-AFBTDTW	1.02	0.99	1.00	0.52	0.98	-0.01	0.00

Experiments - Univariate case

N0	dataset name	N0 of instants	Trend (Y/N)	Seasonal (Y/N)	Frequency
1	Air passenger	144	Y	Y	Monthly
2	Beersales	192	Y	Y	Monthly
3	Google	521	N	N	Daily
4	SP	168	Y	Y	Quarterly
5	CO2 concentrations	160	Y	Y	Monthly
6	Mackey-Glass chaotic	1201	N	N	
7	Phu Lien temperature	648	N	Y	Monthly
8	Water level	131472	N	Y	20 minutes

Imputation performance indicator

Accuracy indexes

- Similarity: the similar percentage between the imputed value (Y) and the respective true values (X)
- NMAE: The Normalized Mean Absolute Error between Y and X
- RMSE: The Root Mean Square Error average squared difference Y and X

Shape indexes

- FSD: Fraction of Standard Deviation between Y and X

Maximum cross-correlation between query and selected windows

-> recurrent patterns

Gap size	dataset							
	#1	#2	#3	#4	#5	#6	#7	#8
6%	0.88	0.92	0.58	0.78	0.99	1	0.91	1
7.50%	0.91	0.91	0.55	0.74	0.99	0.99	0.91	1
10%	0.94	0.87	0.5	0.67	0.98	0.99	0.91	1
12.50%	0.95	0.89	0.44	0.65	0.98	0.99	0.9	1
15%	0.95	0.85	0.4	0.65	0.98	0.99	0.9	1

#1-Airpassenger, #2-Beersales, #3-Google, #4-SP, #5-Co2 concentrations
#6-Mackey-Glass chaotic, #7-Phu Lien temperature, #8-water level

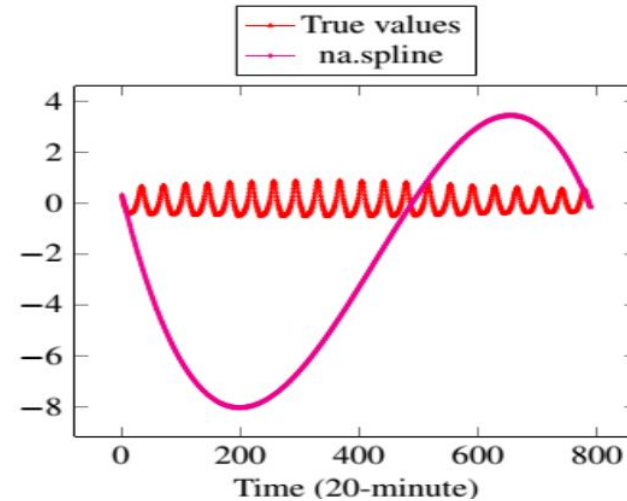
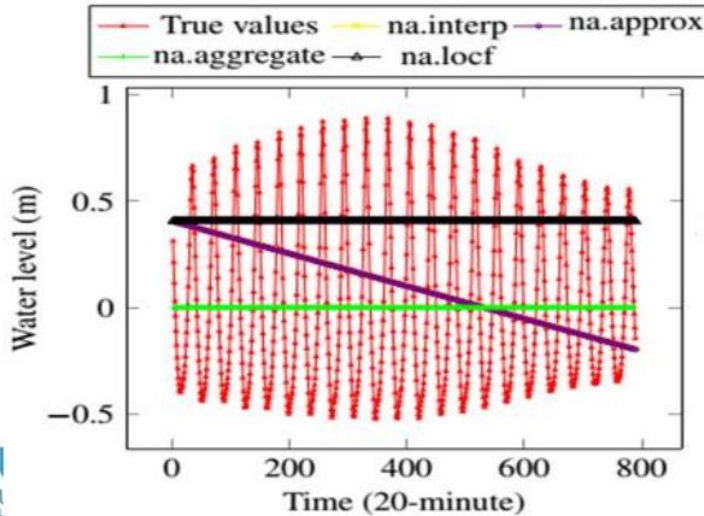
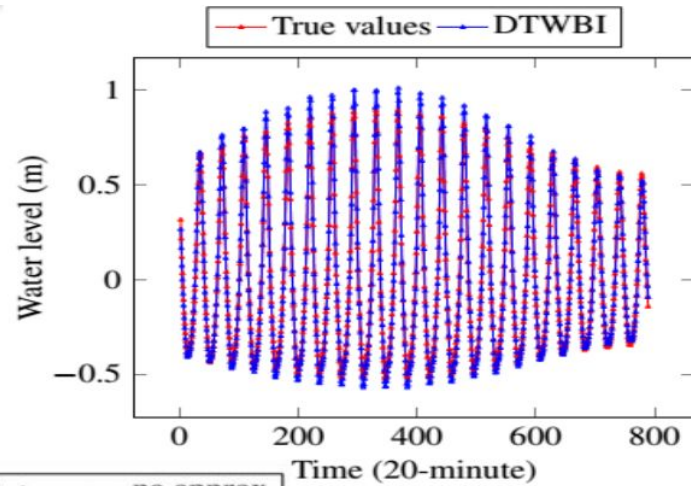
Experiments - Univariate case

Phu Temperature
15% ~ 97 jours

Marel dataset
Gap size/10
1.5% ~ 28 days

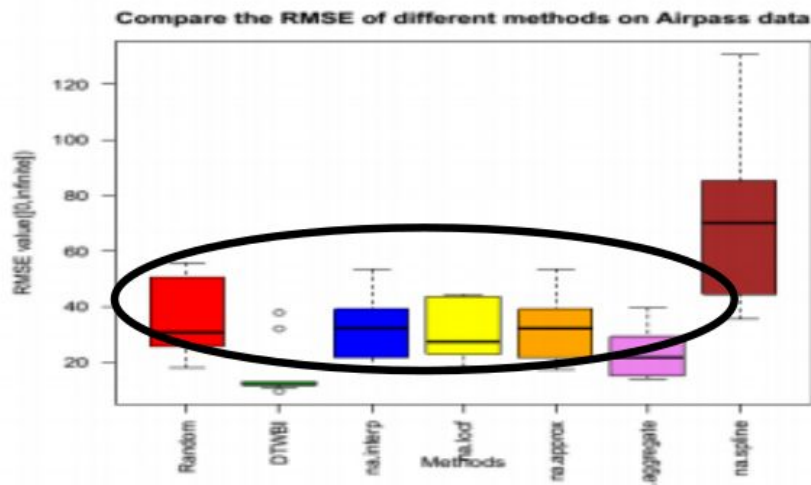
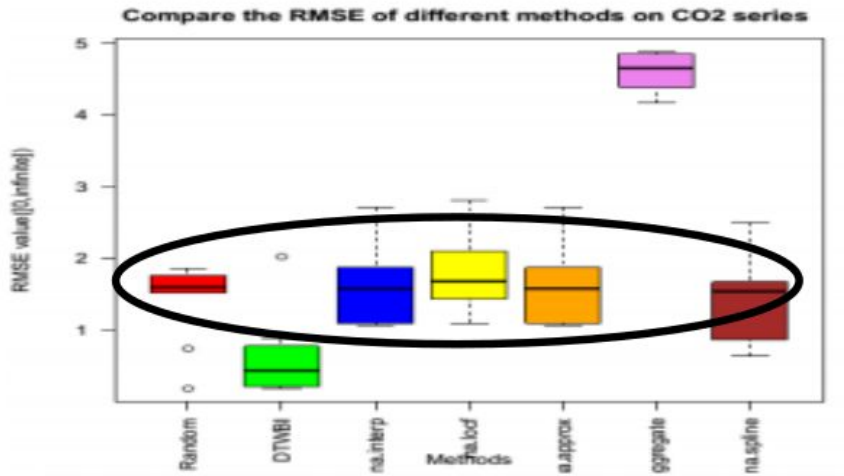
Gap size	Method	CO2 concentrations				Mackey-Glass Chaotic				Phu Lien temperature				Water level			
		Sim	NMAE	RMSE	FSD	Sim	NMAE	RMSE	FSD	Sim	NMAE	RMSE	FSD	Sim	NMAE	RMSE	FSD
6%	DTWBI	0.93	0.001	0.3	0.04	0.95	0.005	0.01	0.03	0.88	0.06	1.7	0.08	0.95	0.009	0.1	0.05
	na.interp	0.75	0.055	1.6	1.5	0.79	0.031	0.04	0.81	0.8	0.142	3.1	0.63	0.81	0.042	0.5	1.05
	na.locf	0.73	0.059	1.7	2	0.77	0.036	0.05	2	0.77	0.173	3.8	2	0.8	0.043	0.4	2
	na.approx	0.75	0.055	1.6	1.5	0.79	0.031	0.04	0.81	0.8	0.142	3.1	0.63	0.81	0.042	0.5	1.05
	na.aggregate	0.45	0.185	4.7	2	0.82	0.025	0.03	2	0.83	0.114	2.4	2	0.83	0.035	0.4	2
	na.spline	0.75	0.057	1.6	0.75	0.65	0.072	0.09	0.38	0.61	0.413	8.5	0.52	0.3	0.654	6.6	1.61
15%	DTWBI	0.94	0.001	0.3	0.04	0.92	0.01	0.02	0.01	0.882	0.066	1.8	0.05	0.96	0.007	0.1	0.04
	na.interp	0.76	0.053	1.6	1.46	0.81	0.03	0.04	0.99	0.81	0.145	3.2	1	0.81	0.044	0.5	1.6
	na.locf	0.77	0.052	1.6	2	0.79	0.037	0.05	2	0.79	0.175	3.8	2	0.81	0.043	0.5	2
	na.approx	0.76	0.053	1.6	1.46	0.81	0.03	0.04	0.99	0.81	0.145	3.2	1	0.81	0.044	0.5	1.6
	na.aggregate	0.43	0.202	5.1	2	0.84	0.025	0.03	2	0.84	0.117	2.5	2	0.83	0.036	0.4	2
	na.spline	0.69	0.085	2.5	0.58	0.57	0.129	0.16	0.73	0.44	1.268	26.3	1.27	0.21	1.185	11.8	1.83
Gap size	Method	Airpassenger				Beersales				Google				SP			
		1-Sim	NMAE	RMSE	FSD	1-Sim	NMAE	RMSE	FSD	1-Sim	NMAE	RMSE	FSD	1-Sim	NMAE	RMSE	FSD
15%	DTWBI	0.1	0.02	12.8	0.36	0.16	0.054	1	0.1	0.15	0.13	0.031	0.29	0.19	0.029	40.7	0.59
	na.interp	0.14	0.025	15.6	0.35	0.11	0.069	0.7	0.17	0.14	0.11	0.031	0.99	0.21	0.033	43.6	0.49
	na.locf	0.21	0.047	28.2	2	0.18	0.126	1.2	2	0.16	0.13	0.034	2	0.19	0.028	36.3	2
	na.prox	0.2	0.043	26.5	1.17	0.17	0.117	1.1	1.42	0.14	0.11	0.031	0.99	0.19	0.032	41	1
	na.aggregate	0.17	0.035	22.1	2	0.16	0.11	1.1	2	0.11	0.08	0.023	2	0.18	0.025	32	2
	na.spline	0.45	0.175	106.1	0.95	0.51	0.731	6.3	0.88	0.66	12.34	2.928	1.6	0.39	0.136	162.5	0.68

Experiments - Univariate case / comparison with random selection

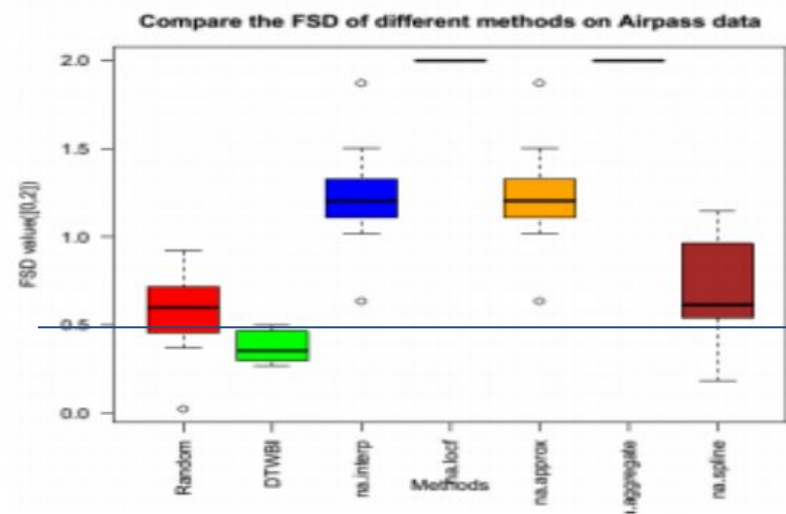
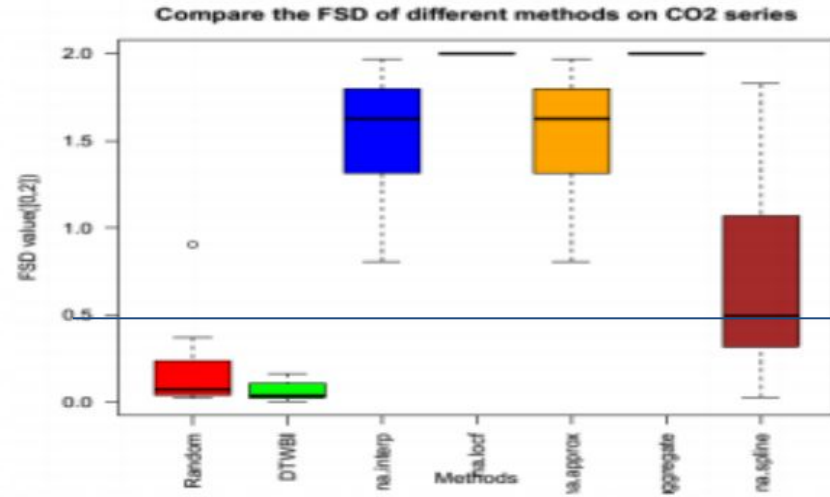


Experiments - Univariate case / comparison with random selection

Efficiency - RMSE ?



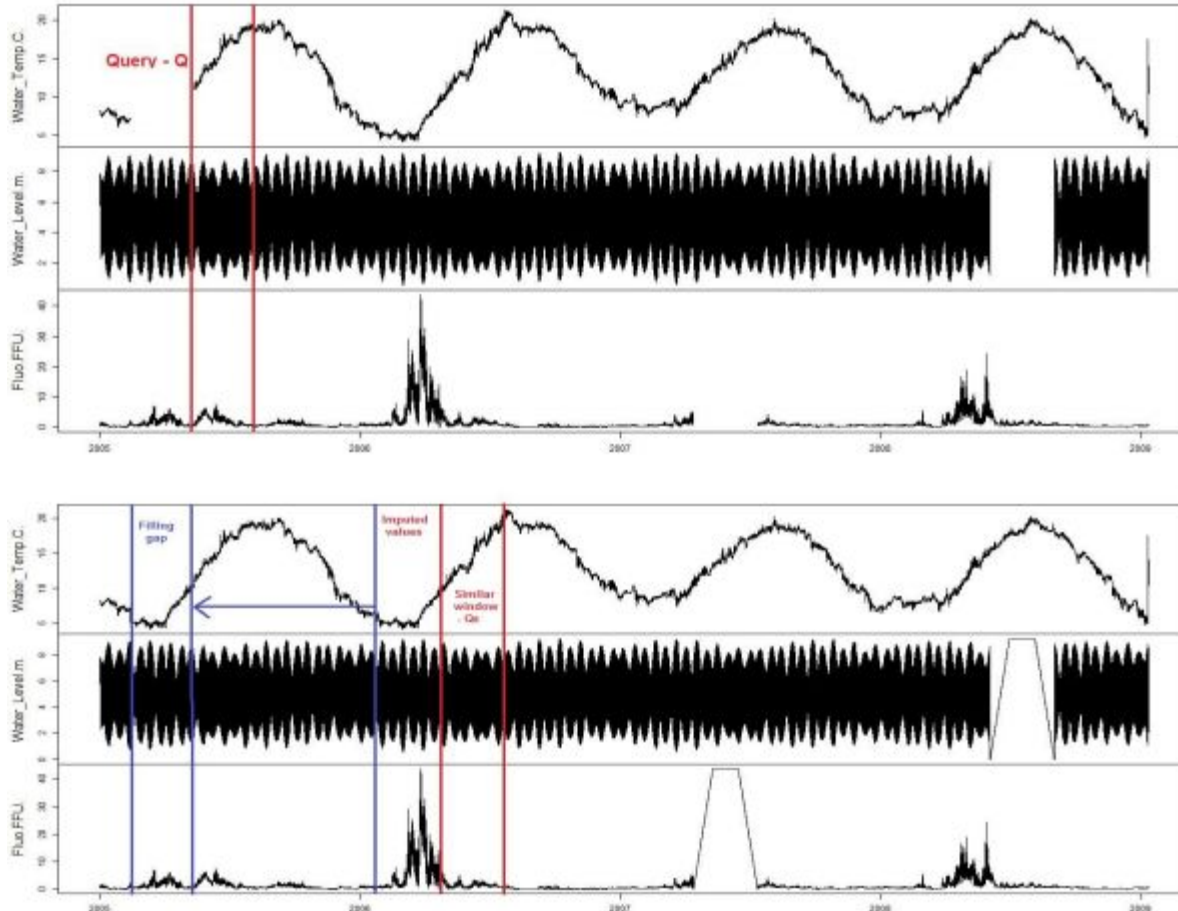
Shape respect - FSD ?



Multivariate dataset

- one-by-one independant filling
- **multivariate similarity**

Extended approach to multivariate signals - DTWUMI



Trapezoid filling of uncomplete signals during the sliding research.

1. Extract shape-features for Q and Reference
2. Select n References satisfying cosine criterion
3. Compute DTW cost of Q and each Reference
4. Select Qs having the the minimum DTW cost
5. Replace the missing values by previous window of Qs on the incomplete signal

Experiments multivariate signals - DTWUMI

N0	Dataset name	N0 of instants	Correlation (No/Low/High)	Frequency
1	NNGC	1,745	High	Hourly
2	Simulation	32,000	No	
3	MAREL-Carnot	35,344	Low	Hourly

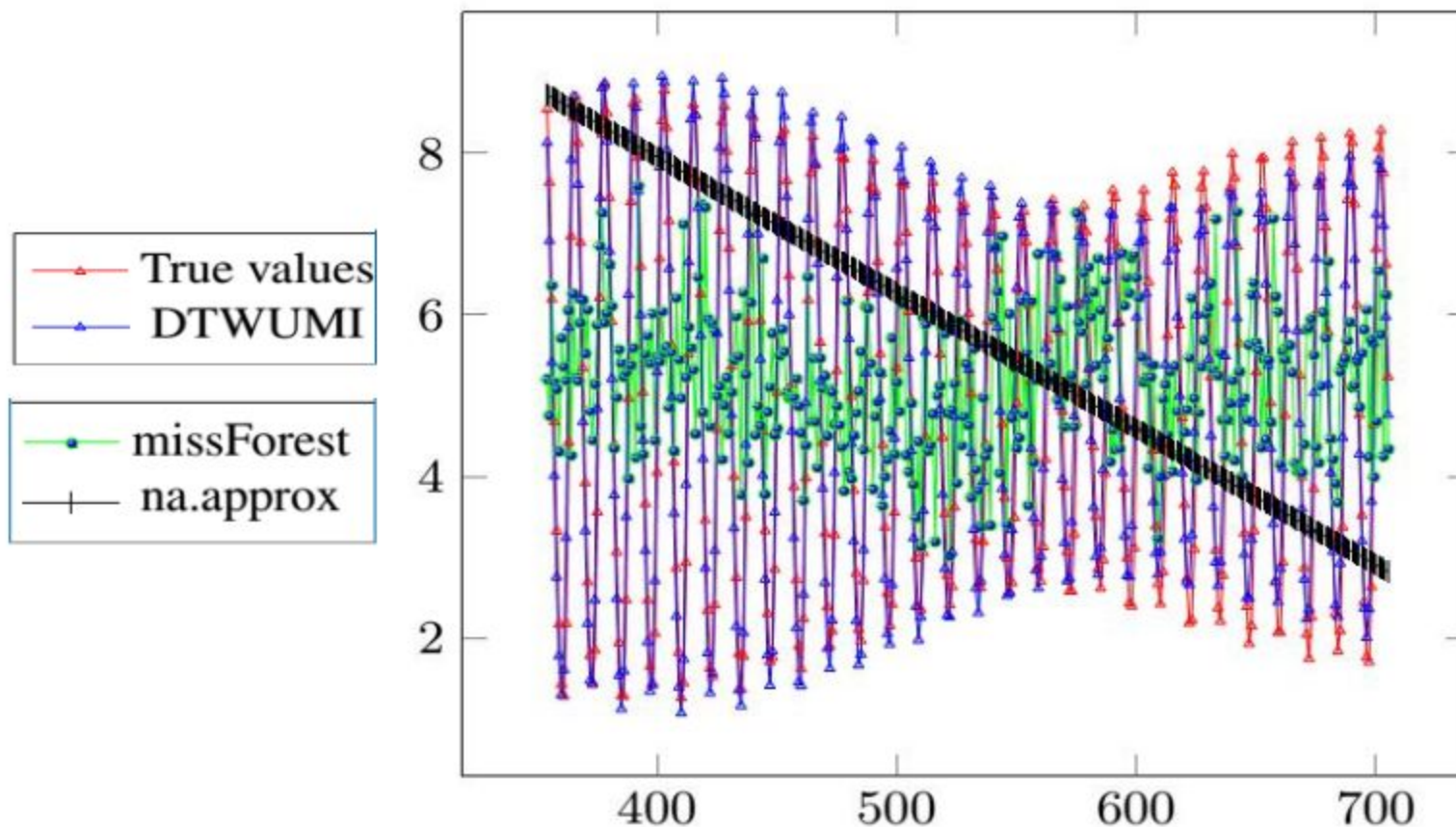
Average imputation performance indexes of various imputation algorithms

Gap size	Method	NNGC dataset						Simulated dataset						Marel CARNOT dataset					
		Accuracy indices			Shape indices			Accuracy indices			Shape indices			Accuracy indices			Shape indices		
		1-Sim	1-R ²	RMSE	FSD	FB	1-FA2	1-Sim	1-R ²	RMSE	FSD	FB	1-FA2	1-Sim	1-R ²	RMSE	FSD	FB	1-FA2
1%	na.approx	0.2	0.99	11786	0.41	0.19	0.52	0.126	0.994	1.99	0.52	1.86	0.81	0.068	0.15	1.62	0.07	0.03	0.21
	MI	0.1	0.32	5774	0.02	0.01	0.26	0.14	0.999	2.22	0.12	1.89	0.79	0.19	0.44	4.48	0.42	0.24	0.48
	MICE	0.03	0.06	2382	0.03	0.01	0.05	0.14	0.997	2.23	0.13	2.39	0.79	0.16	0.46	4.51	0.37	0.2	0.39
	missForest	0.02	0.02	1286	0.01	0.01	0.01	0.11	0.996	1.69	0.89	5.49	0.85	0.15	0.26	3.2	0.35	0.18	0.32
	DTWUBI	0.12	0.51	7591	0.03	0.12	0.3	0.085	0.51	1.22	0.01	5.86	0.58	0.056	0.04	1.02	0.11	0.05	0.15
3%	na.approx	0.18	0.99	11329	0.66	0.29	0.55	0.11	0.998	1.88	0.69	2.08	0.81	0.08	0.17	1.8	0.09	0.07	0.19
	MI	0.1	0.29	5317	0.04	0.02	0.24	0.13	1	2.27	0.03	2.63	0.8	0.21	0.49	4.53	0.41	0.33	0.47
	MICE	0.03	0.11	3112	0.02	0.02	0.05	0.13	1	2.27	0.03	2.63	0.8	0.19	0.53	5.17	0.49	0.36	0.41
	missForest	0.02	0.02	1375	0.02	0.01	0.01	0.1	1	1.71	0.91	2.49	0.85	0.18	0.37	4.09	0.39	0.37	0.36
	DTWUBI	0.05	0.19	4219	0.05	0.08	0.08	0.064	0.45	1.16	0.01	1.72	0.54	0.056	0.06	1.07	0.09	0.02	0.12
10%	na.approx	0.18	1	11419	0.62	0.25	0.56	0.11	1	2.01	0.46	2.02	0.79	0.083	0.23	3.09	0.15	0.16	0.27
	MI	0.1	0.35	5892	0.008	0.02	0.27	0.12	1	2.24	0.02	2.18	0.79	0.13	0.43	4.35	0.16	0.14	0.46
	MICE	0.04	0.13	3435	0.01	0.01	0.06	0.12	1	2.25	0.02	16.56	0.79	0.12	0.5	4.78	0.21	0.18	0.41
	missForest	0.02	0.05	1990	0.02	0.004	0.03	0.09	1	1.7	0.91	1.35	0.86	0.1	0.29	3.47	0.25	0.15	0.3
	DTWUBI	0.05	0.21	4402	0.02	0.04	0.08	0.064	0.47	1.18	0	4.49	0.56	0.065	0.2	2.58	0.12	0.13	0.2

boundary : 1-FA2<0.2 |FB|<0.2 FSD<0.5

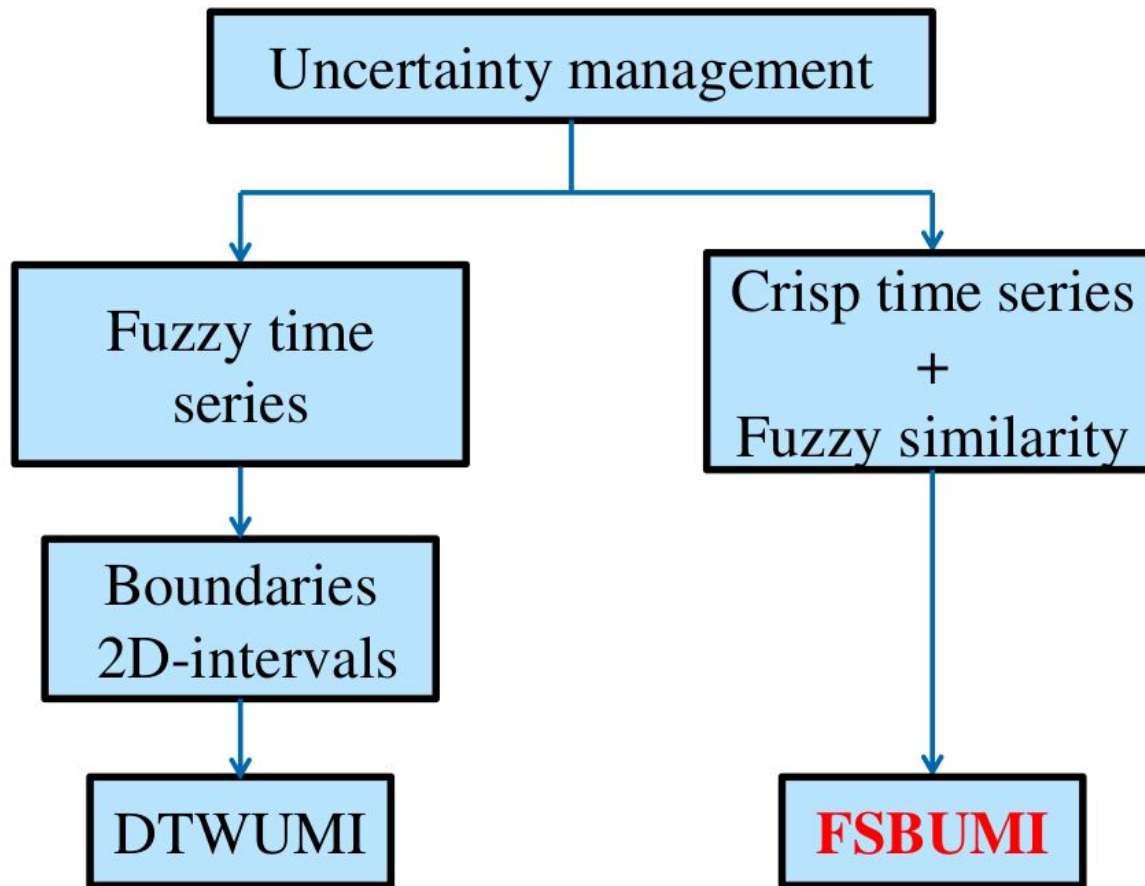
Experiments multivariate signals - DTWUMI

N0	Dataset name	N0 of instants	Correlation (No/Low/High)	Frequency
1	NNGC	1,745	High	Hourly
2	Simulation	32,000	No	
3	MAREL-Carnot	35,344	Low	Hourly

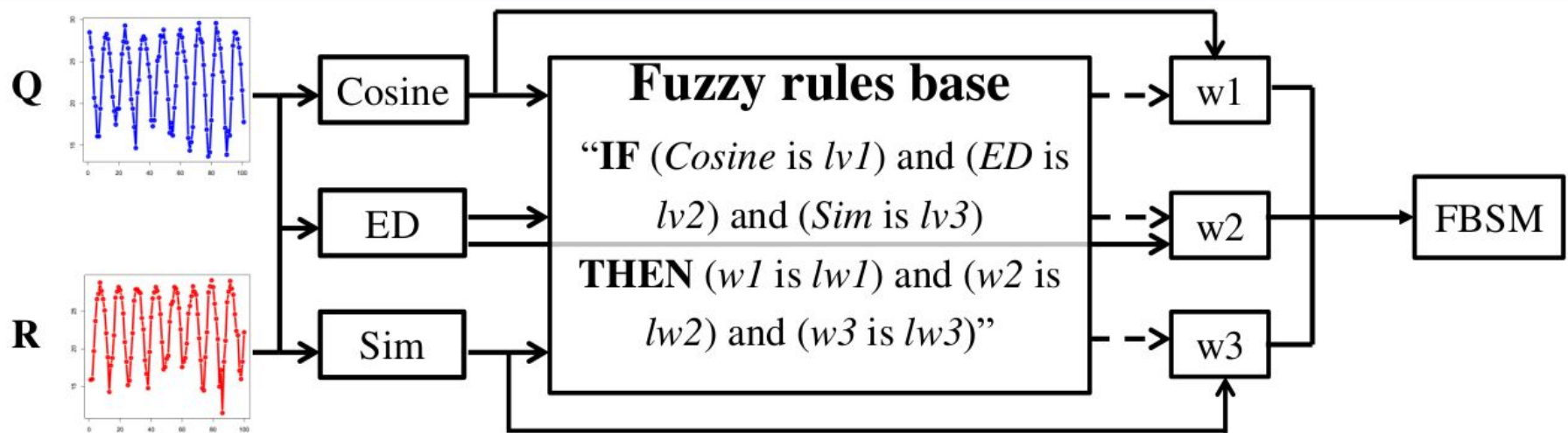


Visual comparison of imputed values of different imputation methods with true values on Marel Carnot dataset with the gap size of 353 on the 2nd signal.

Dealing with uncertainty - speed trade-off

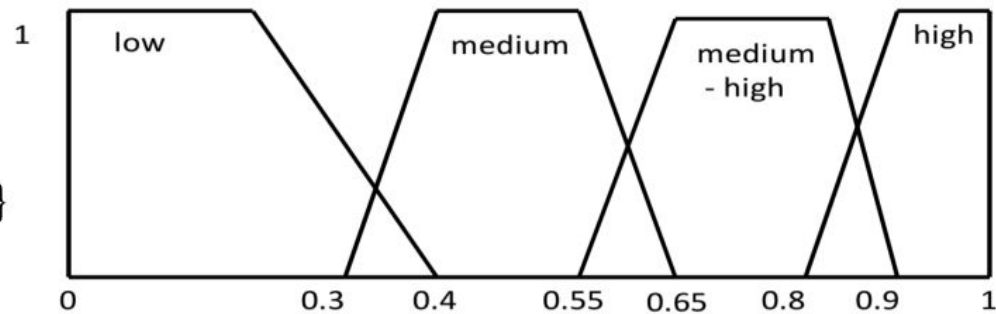


FSBMI scheme. New similarity computation to select best similar windows

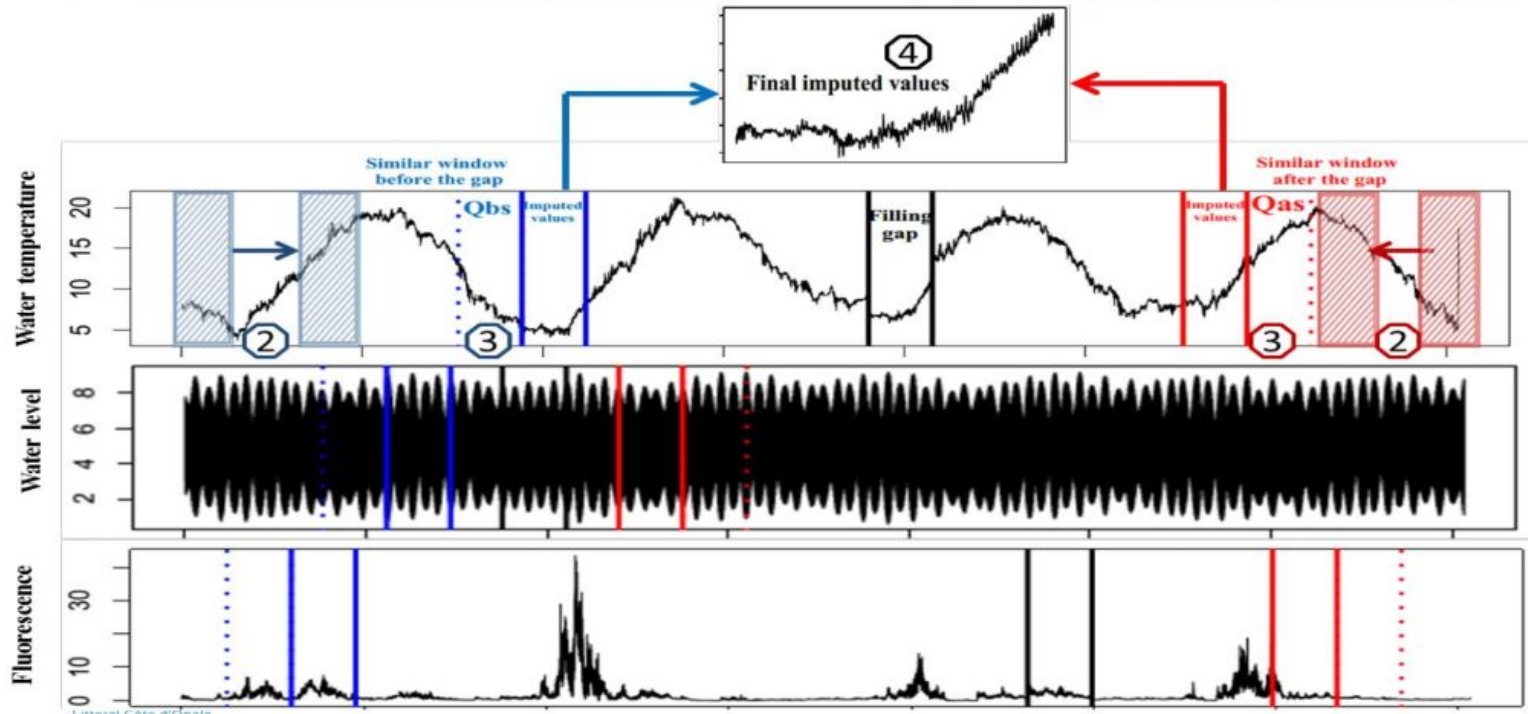
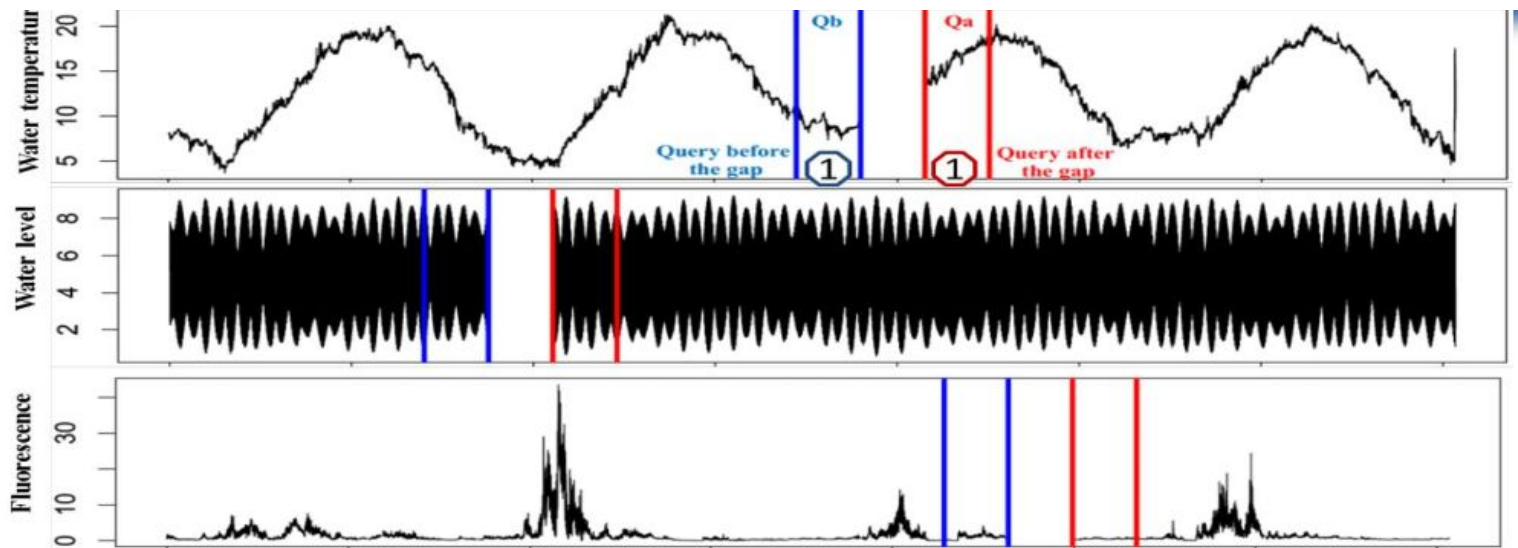


Computing scheme of the new similarity measure

lv: linguistic variable
lw: linguistic weight
 $lv, lw \in \{low, medium, medium-high, high\}$



Membership function of fuzzy similarity values



Simulated dataset (5 signals- 32,000 points)

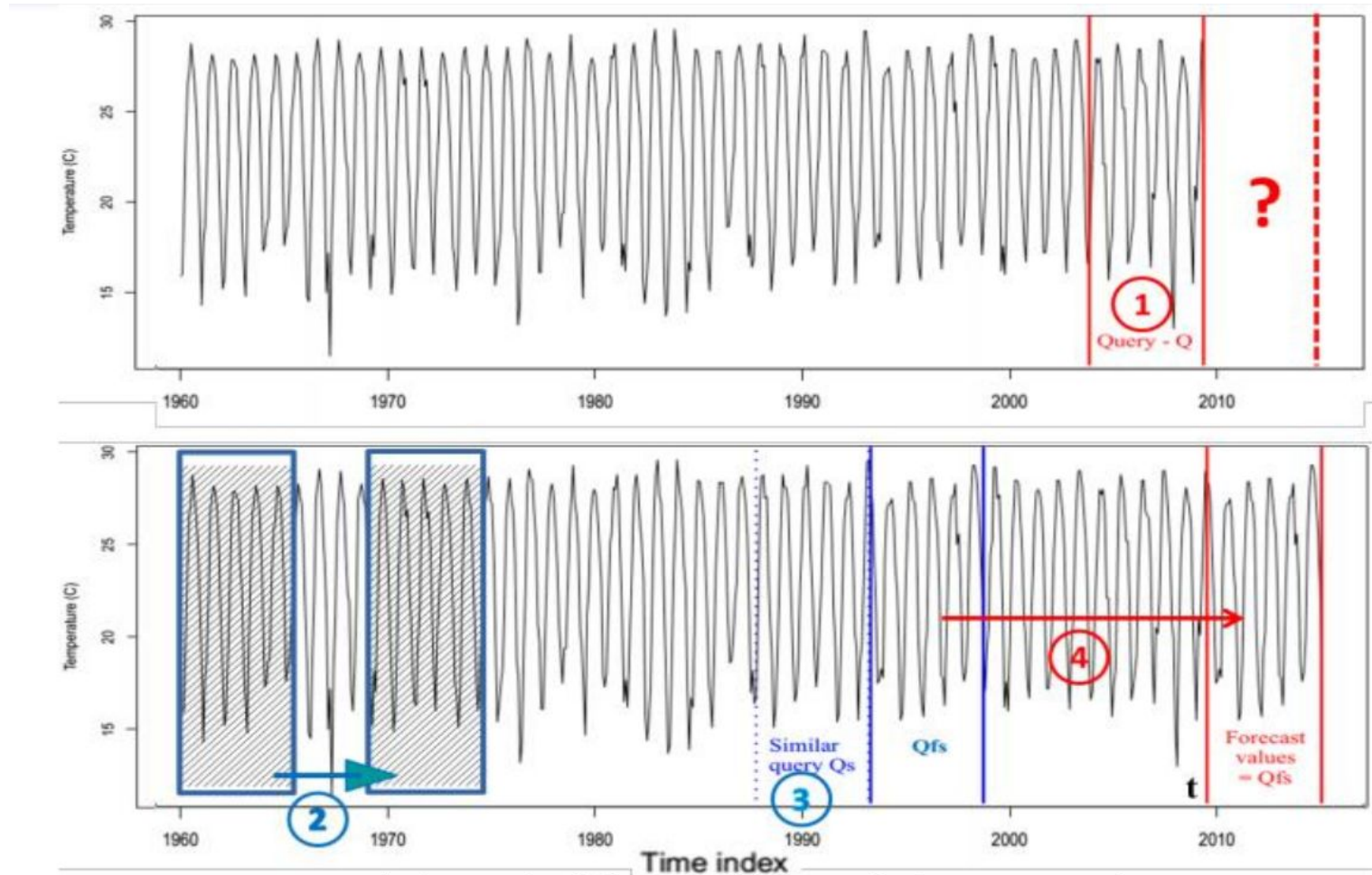
Marel Carnot hourly dataset
(3 signals- 35,334 points)

Gap size	Method	Accuracy indices			Shape indices			Gap size	Accuracy indices			Shape indices		
		1-Sim	1-R ²	RMSE	FSD	FB	1-FA2		1-Sim	1-R ²	RMSE	FSD	FB	1-FA2
7.5%	FSMUMI	0.049	0.071	0.027	0.069	0.505	0.184	4%	0.059	0.058	1.466	0.094	0.101	0.183
	Amelia	0.197	0.998	0.147	0.045	1.305	0.792		0.171	0.44	4.389	0.287	0.2	0.456
	FcM	0.158	0.809	0.104	1.813	1.866	0.991		0.126	0.152	2.779	0.285	0.203	0.727
	MI	0.2	0.992	0.15	0.038	1.645	0.797		0.166	0.41	4.234	0.277	0.204	0.444
	MICE	0.205	0.988	0.15	0.057	10.744	0.799		0.15	0.379	4.15	0.268	0.19	0.411
	missForest	0.188	0.97	0.136	0.284	4.396	0.812		0.129	0.234	3.134	0.23	0.187	0.303
	na.approx	0.192	0.971	0.142	0.669	2.163	0.712		0.077	0.13	2.006	0.068	0.135	0.268
	DTWUMI	0.133	0.653	0.908	0.064	1.113	0.571		0.07	0.105	1.77	0.15	0.12	0.138
10%	FSMUMI	0.061	0.181	0.043	0.114	0.511	0.26	10%	0.053	0.098	1.642	0.083	0.055	0.191
	Amelia	0.202	0.999	0.147	0.034	4.062	0.788		0.14	0.3	4.294	0.24	0.142	0.442
	FcM	0.164	0.872	0.104	1.837	2.201	0.992		0.1	0.098	3.68	0.136	0.101	0.303
	MI	0.21	0.997	0.155	0.12	2.954	0.785		0.14	0.112	4.294	0.24	0.142	0.442
	MICE	0.209	0.996	0.15	0.055	3.994	0.779		0.12	0.42	4.066	0.152	0.077	0.383
	missForest	0.194	0.97	0.135	0.308	3.024	0.811		0.097	0.461	3.049	0.104	0.117	0.255
	na.approx	0.183	0.997	0.129	0.372	1.455	0.719		0.071	0.529	1.873	0.098	0.094	0.253
	DTWUMI	0.155	0.782	0.893	0.026	1.182	0.626		0.081	0.381	3.293	0.119	0.124	0.224

boundary : 1-FA2<0.2 |FB|<0.2 FSD<0.5

Other application: Near Future Prediction

Direct application : DTWBI for Forecasting Univariate TS



**1-Query building, 2-Sliding window comparison,
3-Window selection, 4-Forecasting values**

Documentation



Related Papers.

Univariate time series imputation

- DTWBI - Dynamic time warping-based imputation for univariate time series data. Pattern Recognit. Lett. 139: 139-147 (2020) <https://doi.org/10.1016/j.patrec.2017.08.019>
- eDTWBI - eDTWBI: Effective Imputation Method for Univariate Time Series
Advanced Computational Methods for Knowledge Engineering. ICCSAMA 2019. Advances in Intelligent Systems and Computing, vol 1121. Springer, https://doi.org/10.1007/978-3-030-38364-0_11
- Comparison of DTW variants for the imputation (Ocean'2017), [Which DTW Method Applied to Marine Univariate Time Series Imputation](https://doi.org/10.1109/OCEANSE.2017.8084598) <https://doi.org/10.1109/OCEANSE.2017.8084598>

Uncorrelated multivariate time series imputation

- DTWUMI (MLSP'2017), DTW-Approach for uncorrelated multivariate time series imputation. Machine Learning Signal Processing. <https://doi.org/10.1109/MLSP.2017.816816>
- FSMUMI (ACISC journal - 2018), A New Fuzzy Logic-Based Similarity Measure Applied to Large Gap Imputation for Uncorrelated Multivariate Time Series. <https://doi.org/10.1155/2018/9095683>

Applications to classification and forecasting

- Shape-feature extraction algorithm (ICCE'2016), [Comparative study on supervised learning methods for identifying phytoplankton species.](https://doi.org/10.1109/CCE.2016.7562650) [10.1109/CCE.2016.7562650](https://doi.org/10.1109/CCE.2016.7562650)
- Forecasting meteorological univariate time series (EUSIPCO'2018) [Comparative Study on Univariate Forecasting Methods for Meteorological Time Series.](https://doi.org/10.23919/EUSIPCO.2018.8553576) <https://doi.org/10.23919/EUSIPCO.2018.8553576>

CRAN packages

<https://cran.r-project.org/web/packages/DTWBI/index.html>

<https://cran.r-project.org/web/packages/DTWUMI/index.html>

<https://cran.r-project.org/web/packages/FSMUMI/index.html>

Documentation: <http://mawenzi.univ-littoral.fr/>

Support: emilie.poisson@univ-littoral.fr

Other study:

- GAIN vs DTW-completion
- Adaptive system according signal characteristics (in progress)
- GUI interface (-> 2022)